Special Functions. An Introduction to the Classical Functions of Mathematical Physics

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Errata and Comments

- 1. Page ix, section number 11.4.2 should read: "Asymptotic Expansion; μ Fixed, ξ Large, 302"
- 2. Page ix, section number 11.4.3 should read: "Asymptotic Expansion; ξ Large, μ Arbitrary, 303"
- 3. Page 4, Equation (1.11): include n > 0.
- 4. Page 5, Line 4 and 5: For a proof that the tangent numbers are integers, observe that $y(z) = \tan z$ satisfies the differential equation $y' = 1 + y^2$; hence all derivatives of y at z = 0 are integers.
- 5. Page 16, Line -3: replace = by = -.
- 6. Page 17, Theorem 1.4: include $(-1)^{k-1}$ in the expression for R_k .
- 7. Page 18, Line 4: include (x) in the kth derivative of f.
- 8. Page 26, Exercise 1.11, first line: delete =.
- 9. Page 38, Line 9: "Chapter 10" should read "Chapter 9".
- 10. Page 43, Section 3.2, Line 6-9: ... is analytic in the half-plane $\Re z > -1$ with 0 excluded. The question about the nature of the singularity at 0 is answered as follows: from $\Gamma(z) = \Gamma(z+1)/z$ and $\Gamma(1) = 1$ we see that the origin is a pole of first order.
- 11. Page 45, Section 3.2.3, Line 7: read $\frac{1}{2}\Gamma(p)$.
- 12. Page 49, Line 2 from the bottom: /q should read $/\pi$.
- 13. Page 49, Bottom line: in the first fraction, the numerator should read π and not q.
- 14. Page 50, Line 2: replace "term" by "factor"

- 15. Page 52, Lines 8 and 9: The product sign must be moved to the numerator of the subsequent fraction (both in Line 8 and Line 9)
- 16. Page 52, Line -1: in the numerator of the middle part replace $(mn/e)^m n$ by $(mn/e)^{mn}$.
- 17. Page 71, Line -8: the summation should start with n = 1.
- 18. Page 74, 3.9: replace $e^{-\pi|y|}$ by $e^{-\pi|y|/2}$.
- 19. Page 74, Bottom line: in the first fraction, the denominator should read π and not q.
- 20. Page 76, Line -3: replace "for a start" by "for convergence".
- 21. Page 77, Line 5: replace $\Re z > 1$ by $0 < \Re z < 1$.
- 22. Page 80, Line 12: u(u, y, z, t) should read u(x, y, z, t).
- 23. Page 98, Bottom line: insert "=" after the sum.
- 24. Page 103, Equation (4.41) and in the second line below this equation: replace τ by t.
- 25. Page 131, Exercise 5.11: read n = 0, 1, 2, ...
- 26. Page 142, Line 4: read A and B do not...".
- 27. Page 151, include the factor $2\pi i$ in the denominator in front of the integral.
- 28. Page 152, Equation (6.39), denominator of the third line: Replace 2^k by 2^n
- 29. Page 159, Line 2: replace "It is easily verified that" by "Introducing in (6.55) the new variable of integration $u = 1 e^{-t}$, we easily verify that"
- 30. Page 170, Exercise 6.18, the subscript in the Laguerre polynomial in the sum should read k and not n .
- 31. Page 171, Bottom, replace the \sim by "=" (two times) and include +o(1) after the sine and cosine terms.
- 32. Page 173, Line before (7.7): Rec should read $\Re c$.
- 33. Page 180, Line 2 after (7.23): include $\frac{2}{\sqrt{\pi}}$ in front of the M-function and $\frac{1}{\sqrt{\pi}}$ in front of the U-function.
- 34. Page 181, Line 2, 3 and 4 (formula for Ei(z)) should be skipped.
- 35. Page 181, Second line below this: (7.24) should read (7.25).
- 36. Page 182, Middle of the page: the number 1.089490... should read 1.1789... (twice).
- 37. Page 186, In subsection 7.3.8, Line 4: replace $\exp(iz)$ by $\exp(-iz)$.
- 38. Page 186, Middle, point 7.1: "Buchholtz" should read "Buchholz"; the same correction is needed in the Index on page 366.
- 39. Page 190, Line 4: z^s should be z^{-s} .
- 40. Page 201, Equation (8.33): lower limit of integration should read -1.
- 41. Page 222, Equation (9.6), second formula: replace the fraction $\frac{1}{2\pi i}$ by $\frac{-1}{2\pi}$.
- 42. Page 232, Line 8 from bottom: "Batemann" should read "Bateman".
- 43. Page 236, Equation (9.44): $(2/z)^{\nu}$ should read $(2z)^{\nu}$. The result holds for $\Re z > 0$ and $\Re \nu > -1/2$.
- 44. Page 236, Line after (9.44): "(6.12)" should read "(7.12)".
- 45. Page 247, Line 2 from bottom: "(3.13) and (3.14)" should read "(4.13) and (4.14)".

- 46. Page 253, Line 6 from bottom: "Remark 9.2" should read "Remark 9.4".
- 47. Page 255, Lines 7 and 8: replace the \sim by "=" (two times) and write $[\cos(\zeta \pi/4) + o(1)]$ and $[\sin(\zeta \pi/4) + o(1)]$ for the cosine and sine terms.
- 48. Page 260, Line 6 from bottom: F_{ϕ} should read (rF_{ϕ}) .
- 49. Page 273, Exercise 10.3. Replace the words "current density" by "charge density" (two times).
- 50. Page 279, Line 4 after (11.9). Replace |a/z| by |z/a|.
- 51. Page 283, t-integral: include $0 < c < \lambda$.
- 52. Page 284, Line before (11.21): "non-negative" should read "non-positive".
- 53. Page 285, Line -5: write u(t) = -i(t-1).
- 54. Page 289, Line before $\S11.3.1$: " $\S11.3.6$." should read " $\S11.3.4$ ".
- 55. Page 298, Equation (11.60). Replace π by 2π (two times).
- 56. Page 299, Equation (11.64). Replace e^{-x} by e^{-x-y} .
- 57. Page 301, Line before Equation (11.71). Replace s=1 by t=1.
- 58. Page 304, Equation (11.81). Replace \sinh , by $\sinh \gamma$,.
- 59. Page 315, Equation (12.1): $0 \le k < 1$.
- 60. Page 315, Equation (12.2): $0 \le k \le 1$.
- 61. Page 321, Equations (12.15), (12.16), (12.17): ϕ should be restricted to the interval $[-\pi/2, \pi/2]$ and k as in (12.1) and (12.2). After (12.20) insert: "If n > 0 and $x^2n > 1$ the integral in (12.20) should be interpreted as a Cauchy principal value integral."
- 62. Page 325, Line -5, series for θ_4 : the exponential function should read e^{2niz} .
- 63. Page 346, Eq. (13.13): replace $\frac{1}{2}$ by $\frac{1}{s}$.
- 64. Page 353. Include item: G. Gasper and M. Rahman (1990), Basic hypergeometric series, Cambridge University Press, London and New York.
- 65. Page 353. Include item: W. Gautschi (1994), Algorithm 726: ORTHPOL A package of routines for generating orthogonal polynomials and Gaus-type quadrature rules, $ACM\ Trans.\ Math.\ Softw.,\ {\bf 20},\ 21-62.$