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Positive streamers in air of varying density: experiments on the scaling of the excitation density

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Abstract

Streamers are rapidly extending ionized finger-like structures that dominate the initial breakdown of large gas volumes in the presence of a sufficiently strong electric field. Their macroscopic parameters are described by simple scaling relations, where the densities of electrons and of excited molecules in the active streamer front scale as the square of the density of the neutral gas. In this work we estimate the absolute density of nitrogen molecules, excited to the C\textsubscript{3}Π\textsubscript{u} state that emit photons in the 2P–N\textsubscript{2} band, by radiometrically calibrated short exposure intensified imaging. We test several pressures (100, 200 and 400 mbar) in artificial air at room temperature. Our results provide a first confirmation for the scaling of the density of excited species with the gas density. The method proposed here is particularly suitable to characterize the excitation densities in sprite streamers in the atmosphere.

Keywords: streamers, radiance, excitation density, sprites, electron density

(Some figures may appear in colour only in the online journal)

1. Introduction

The initial breakdown of large gas volumes is dominated by rapidly extending ionized finger-like transient structures known as streamers, which occur in the presence of a sufficiently strong electric field. They appear on a large scale in the mesosphere, where they are observed in sprites, and on a smaller scale in streamer discharges created in laboratory settings at standard atmospheric density. Streamer discharges have the appearance of a tree-like structure, with streamers branching to all sides from a few main channels (recently modelled by Luque and Ebert [1]). The macroscopic parameters of streamers are described by simple scaling relations; the electric field in the streamer scales as the neutral density \( N \), the diameter as \( 1/N \), and the densities of produced species (such as free electrons, ions, radicals and excited molecules) scale as \( N^2 \) [2–5]. Streamer diameters, velocities and inferred electric fields, measured in the laboratory at close to standard temperature and pressure were shown to scale with gas density to sprite streamers [6–9].

The absolute densities of the various species \( n_x \) produced by the passage of streamers in pure nitrogen and air were measured with several methods, typically at standard pressure (see e.g. [10–17]). The parameter which is typically estimated in these measurements is the bulk production of active species. The volume of gas treated by a streamer discharge is estimated using the number of streamers and their mean diameter, as derived from images of the entire discharge. The density of excited molecules (the excitation density) produced by a single streamer is then estimated as the ratio between the bulk production and the average volume treated by the discharge, which consists of numerous streamers. Šimek \textit{et al} [12] estimate the
density of the N₂ (A³Σ_u⁺) and N₂ (C³Π_u) excited states, produced by the passage of a streamer discharge in high purity nitrogen (quality not specified) and their decay over time, using the Herman infrared emission (HIR) technique. They estimated the excitation densities a short time after the discharge, finding ~5 × 10¹⁴ cm⁻³ at ~1 μs after the discharge and ~10¹³ cm⁻³ less than 0.1 μs after the discharge, respectively. Ono et al [15] used the Laser-Induced Fluorescence (LIF) technique to estimate that the density of N₂ (A³Σ_u⁺) created in the path of a streamer in pure nitrogen is ~6 × 10¹³ cm⁻³. That work was followed by Teramoto et al [16], who estimated the absolute density of N₂ (A³Σ_u⁺) in nitrogen with trace amounts of additives and found that while in pure nitrogen the absolute density is 2 – 3 × 10¹³ cm⁻³, when more than 0.1% oxygen is added the excitation density grows to ~4 × 10¹³ cm⁻³. They also found that the density of the excited molecules increases by a factor of 2 when the applied voltage increases from 18.5 to 21.5 kV. Naidis [18] reexamined these experimental results, taking into account the strong radial non-uniformity of plasma parameters in the streamer channel. His estimation of the initial number density of N₂ (A³Σ_u⁺) on the axis of the streamer was ~4 – 9 × 10¹⁴ cm⁻³. Pancheshnyi et al [10] measured the excitation densities of several excited states, among them the N₂ (C³Π_u) state, by analyzing the emission spectrum along the path of the discharge. They estimated that the maximum linear density of the N₂ (C³Π_u) excitations was 0.5 – 1.0 × 10¹⁰ cm⁻¹. The radius of a streamer can vary by an order of magnitude when the applied voltage is doubled [19]. Assuming, for the sake of argument, that the streamer diameter is 0.4 mm (not a minimal streamer) at standard pressure the excitation volume density can be estimated as 4 – 8 × 10¹² cm⁻³. Additional insight can be gained from the guided streamers (plasma bullets), recently reviewed by Lu et al [20]. Experimental estimations of the electron density in the streamer column of the plasma bullet are 2 × 10¹³ cm⁻³ [21] and 10¹¹–10¹³ cm⁻³ [22]. Unlike the streamers discussed in this work, guided streamers follow a known trajectory determined by pre-ionization, which is achieved by a laser beam or a thin column of a plasma jet injected in the discharge gap.

The production of various excited species and the increase of the electron density due to the passage of a streamer were simulated in several papers [3, 23–33], to name but a few, most of which agree that the electron density on the axis of the streamer is on the order of 10¹³–10¹⁴ cm⁻³. In general, the density of the excited species on the streamers axis will depend both on the neutral gas density and on the maximal electric field at the streamer tip. Naidis [23] and later Li et al [34] proposed an approximation for the production of species, expressed as:

\[ n_x = \frac{60}{e} \int_0^{\frac{1}{2}} \alpha_x(E) dE \]

where \( n_x \) is the density of produced species, \( \alpha_x \) is the inverse ionization or excitation length and \( IE^{\frac{1}{2}} \) is the maximal electric field ahead of the streamer front. Using (1) it is easy to see that the densities of many species on the axis of the streamer are of the same order of magnitude as the density of free electrons, and all depend on the locally enhanced electric field. Naidis [8] reviewed previous work and found that the maximal electric field at the streamer head in laboratory settings at 1 bar is 120–160 kV cm⁻¹, corresponding to 480–640 Td (1 Td = 10⁻¹¹ V·cm⁻²). The densities of several excited species, calculated with equation (1), are plotted in figure 1. This plot shows the densities produced by electron impact excitation during the passage of a streamer. The electron density and the N₂ (C³Π_u) density vary by a factor of 4–5 in this range, with 2–7 × 10¹³ and 0.6–1.0 × 10¹³ cm⁻³ respectively. It should be noted, that in our experiments, we do not observe streamers which are wider than 2 mm bar. With this limitation the electric field fits into a smaller range than proposed by Naidis [8], 120–140 kV cm⁻¹ (480–560 Td), where the densities vary by a factor of two.

As the excited molecules decay to lower states, the densities of low lying excited states increase. The second positive system (2PN₂) is the result of the transition C³Π_u → B³Π_g, occurring on the time scale of 50ns; the B³Π_g state decays in turn into the A³Σ_g state, while emitting in the first positive system (1PN₂), on the time scale of ~6μs. The A³Σ_g state decays on the time scale of 1 μs. The plot in figure 1 represents the initial excitation densities, not including subsequent transitions. Time scales are taken from Kuo et al [35].

2. Scaling of excitation densities

The processes that drive streamer propagation are determined primarily by two-body interactions, the collisions of free electrons with heavy molecules (in weakly ionized plasmas, collisions with ions or other electrons are rare). The length scale of the discharge process in the streamer tip is the mean free path of electrons. Since electrons collide mostly with neutral molecules, the mean free path of
electrons is inversely proportional to the neutral number density \(N\). Therefore all lengths and times determined by electron motion scale like \(1/N\). The electric field in front of the streamer head follows the Townsend scaling relation, \(E \sim N\). The Poisson equation leads to the scaling relation of the charge density, \(\rho = V E / d\), so that the charge density, the density of electrons and ions, as well as the density of the products of electron-molecule collisions, all scale with \(N^2\). The topic of scaling relations in streamers is discussed in detail by Ebert et al [39]. We do not treat photo-ionization here, as several works demonstrated that this effect can be neglected at ground pressure. Photo-ionization may result in the breaking of scaling when laboratory streamers are compared with sprites [25, 30, 40].

Scaling of streamer diameters and velocities was demonstrated in experiments in air and in other gas mixtures [7, 27, 40, 41]. The density of molecules excited by the passage of a streamer is related to the amount of light emitted in the streamer head. Therefore it is possible to test the scaling of excitation densities, and estimate their absolute value at different pressures using calibrated radiometrical measurements. Pancheshnyi et al [27] measured the integral radiation of a streamer discharge as a function of pressure (in relative units). They found that as pressure increases from 300 to 760 Torr (400–1000 mbar), the emission intensity decreases, indicating that the total production of \(N_2(C^3Π_u)\) increases with decreasing pressure. According to Ebert [39], the excitation and electron density integrated over the streamer head scales like \(1/N\).

Streamers are a transient phenomenon, observed optically as the passage of a bright front, the streamer head, propagating at velocities between \(10^5\) and \(10^7\) m s\(^{-1}\) [9, 19, 26, 41, 42]. As the streamer propagates in the discharge gap, passing in the field of view of the camera, it illuminates several pixels in the image for less than 1 ns (and only a few microseconds in sprites), typically only a fraction of the camera exposure time. We do not use the more common measure of radiance in Rayleigh units as this quantity requires knowledge of the illumination duration, which is typically shorter than the exposure time in our experiments, as well as in sprite observations. If a source is well resolved spatially, but not well resolved temporally, radiance measurement will depend on the exposure time, as was demonstrated in [26]. Therefore the relevant quantity when discussing the brightness of streamers is the time-integrated radiance (TI-radiance), a measure of the total number of photons emitted from a gas volume into a cone defined by a unit area and a solid angle.

In this work we test the scaling of the density of excited molecules, created by the passage of primary positive streamers in a point plane discharge gap. We measure the radiance and diameters of individual streamers and estimate the excitation density of nitrogen molecules in the \(C^3Π_u\) state, at several pressures (e.g. 100, 200 and 400 mbar) in artificial air at room temperature. This state emits photons in the second positive band of \(N_2\) (the implication of a non-uniform radial distribution on the average production of many streamers. To our knowledge this has never been tested experimentally.

Assuming that emitting molecules radiate isotropically and are distributed uniformly in a cylindrical volume, and the streamer is optically thin, then the maximum TI-radiance of a streamer is the density of photon-emitting molecules integrated along the line of sight through the center of the cylindrical volume:

\[
L_1 \sim d n^* Q / 4\pi
\]  

where \(d\) is the optical (observed) diameter of the streamer, \(n^*\) denotes the density of the excited molecules, \(Q\) is the fraction of the excited molecules that undergo radiative relaxation, and the factor \(4\pi\) accounts for isotropic emissions. In the experiments described here the optical emissions are dominated by the \(2P\) band in the near UV, created by the transition \(C^3Π_u \rightarrow B^3Π_g\) [10]. Some of the excited molecules lose their energy through collisional de-excitation by other molecules. The quenching factor \(Q = (1 + N/N_q)^{-1}\) is the fraction of excited states that emit photons. Here \(N\) is the neutral density and \(N_q\) is the quenching density. For the \(N_2(C^3Π_u)\) state \(N_q\) is \(2.9 \times 10^{17}\) cm\(^{-3}\), equivalent to \(p_q = 12\) mbar at standard temperature. When the neutral density is equal to the quenching density half of the excited molecules emit photons. We used the values listed in Kuo et al [35].

It is possible to measure the TI-radiance and the streamer diameter, and derive the density of excited species as

\[
n^* \sim 4\pi L_1 / Q d
\]  

If \(n^*\) does not depend strongly on the thickness of the streamers, then \(L_1\) depends linearly on diameter. According to an analysis by Naidis [8], based in part on measurements by Briels et al [19] and Winands et al [42], the reduced electric field in the streamers’ heads does not depend strongly on the diameter of the streamers. In our setup, which follows [19], we do not observe streamers with reduced diameters wider than 2 mm bar, which makes us conclude that the electric field in the streamer head is fairly constant. It is therefore reasonable to expect a weak dependency of \(n^*\) on the diameter. In the present analysis we neglect the non-uniform radial distribution of \(n^*\) in the streamer channel (the implication of a non-uniform radial distribution on streamer emissions is discussed in detail by Nudnova and Starikovskii [43]).

3. Experimental methods

A complete description of the experimental setup can be found in [40, 44] and will be repeated here briefly. We create positive streamers in a 16 cm point-plane gap, contained within a large cylindrical stainless steel vacuum vessel, specifically designed to maintain the purity of the enclosed gases. The vessel is filled with artificial air, \(N_2: O_2–80%: 20\%\), the pressure is controlled in the range of 100–1000 mbar at room temperature. We used three different pressures: 100, 200 and 400 mbar. A high voltage pulse was generated by a so called C-supply, described fully by Briels et al [44]. It has a 10–90%
rise time between 70 and 120 ns and a fall time of about 10 μs. The peak of the voltage pulse can be set to values between 10 and 40 kV. The higher voltage peaks typically result in the formation of thicker streamers near the needle electrode and in the discharge gap.

A quartz window is installed in the vacuum vessel to allow viewing and recording of the discharge. The vessel and circuit are placed in an external Faraday cage which protects the delicate imaging equipment, with a viewing window made of a fine wire mesh grid to complete the Faraday cage. The fine mesh grid window is equally transparent to all wavelengths in the visible and the near UV range, transmitting ~52% of the light.

The streamers are imaged using a Stanford Computer Optics 4QuickE intensified CCD camera, with nanosecond exposure time, mounted with a UV-Nikkor 105 mm lens, sensitive to wavelengths in the range 120–850 nm. The imaging setup was calibrated using a tungsten ribbon lamp, as described in the appendix.

The estimation of the brightness of a streamer is illustrated in figure 2: a straight isolated streamer channel section is selected in the image. Several perpendicular cross sections along the chosen streamer are averaged to obtain a single curve, as shown in figure 2(b). The streamer diameter is determined as the full width at half maximum (FWHM) of the peak. A rectangular region of interest (ROI) is chosen along the streamer center, with width FWHM (dashed box in figure 2(a)). An average gray level (GL) value is calculated within the ROI. Assuming the GL is distributed as a Gaussian in the radial direction, the average GL determined in this manner is about 80% of the value determined at the peak. The background gray level (GL₀) is determined using two ROI parallel and outside of the streamer section with the same dimensions (solid boxes in figure 2(a)). A similar method to determine the background signal was used by Yaniv et al [45]. Several hundred streamer sections were analyzed in this manner at each pressure.

The camera was moved on an optical rail to one of three positions, with different distances from the discharge vessel (indicated in table 1 as R). The position of the camera determines the instantaneous field of view (IFOV), the magnification, and critically, the depth of field. The radiance of an extended source on the other hand, does not depend on the position of the camera. Streamers in our analysis are wider than 10 pixels, and can be considered as extended sources. The depth of field describes how far from the focal plane an object can be placed to appear focused in the image. It depends on the resolution of the camera and the distance from the object. The estimated values depths of field are listed in table 1. When the depth of field is narrower than the volume of the vessel, many streamers are out of focus. As a result their image on the CCD appears wider, and the measured diameter is overestimated. It is usually impossible to distinguish between streamers that are in focus and those that are not. On the other hand, if the camera is positioned far from the discharge, increasing the depth of field, the imaged streamers are too narrow to be resolved. To overcome these

Table 1. Camera zoom settings and related optical lengths. R is the distance between the front of the camera and the needle electrode, DoF is the depth of field, calculated for a circle of confusion of 10 pixels and m is the magnification. The error in magnification is representative of the estimation error of FWHM.

<table>
<thead>
<tr>
<th>Zoom</th>
<th>R [mm]</th>
<th>DoF [cm]</th>
<th>m</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max</td>
<td>620</td>
<td>1.6</td>
<td>0.28 ± 1.6%</td>
</tr>
<tr>
<td>Mid</td>
<td>1130</td>
<td>8</td>
<td>0.12 ± 0.6%</td>
</tr>
<tr>
<td>Min</td>
<td>2050</td>
<td>30</td>
<td>0.06 ± 4%</td>
</tr>
</tbody>
</table>

Figure 2. (a) A short exposure image of a streamer in dry air, rendered in false color. Rectangles indicate the regions of interest used to find the mean gray level of the streamer (GL, dashed), and the background (GL₀, solid). (b) The mean cross section of the streamer in (a). The full width at half maximum (FWHM, confined by two vertical lines) of the cross section determines the width of the region of interest. GL₀ is indicated by the horizontal line.
limitations we used several camera positions, indicated by min, mid and max zoom in table 1 and figure 3.

Sample images at various voltage settings and camera positions are shown in figure 3. At the minimum zoom setting the entire discharge volume is observed, with the needle at the top of the image. Streamers emanate either from the tip of the needle or from sharp edges above it. The latter do not typically propagate in the direction of the plate, and are not included in the analysis below. The plate is located at the bottom of the image (a weak reflection of the discharge can be observed there). At the max zoom setting neither electrode appears in the image. The depth of field is narrow, with an obvious example in 400 mbar, 30 kV.

Figure 3. Sample images of streamer discharges at 200 and 400 mbar. The columns correspond to applied voltages as indicated above. The rows correspond to pressures and zoom settings. The gain voltage and exposure time are indicated in each image. At the min zoom setting the entire discharge volume is observed, with the needle at the top of the image. Streamers emanate either from the tip of the needle or from sharp edges above it. The latter do not typically propagate in the direction of the plate, and are not included in the analysis below. The plate is located at the bottom of the image (a weak reflection of the discharge can be observed there). At the max zoom setting neither electrode appears in the image. The depth of field is narrow, with an obvious example in 400 mbar, 30 kV.

4. Results

In figure 4 we plot the time-integrated radiance $L_t$ as function of the reduced diameter $pd$ for each pressure. We find a positive correlation between $L_t$ and $pd$ in the three datasets, with the linear Pearson coefficient between 0.6 and 0.7 (see table 2). In figure 4(a) measurements at all three pressures overlap, implying that the radiance of streamers at different pressures but similar conditions, follows a similar trend.

To test whether the time integrated radiance depends linearly on diameter, as expected, we perform a linear fit to the log–log plot of $L_t$ versus $pd$ (figures 4(b)–(d)). The slope $\alpha$ is the exponent in the relation $L_t \sim (pd)^\alpha$, and we expect $\alpha = 1$. The fitting results are listed in table 2. We find that $\alpha < 1$, seemingly indicating that less light (photons) is emitted from thicker streamers. However this less-than-linear dependence can also be explained by the setup limitations: when the camera is close to the discharge, its depth of field is very narrow. Streamers which are not in the focal plane may appear wider, leading
to an overestimation of their diameter. On the other hand as long as the image of an out of focus streamer is not extremely blurred, the radiance measurement on its central axis should not be significantly affected. This would cause some of the data points to appear below the expected linear trend line.

The density of excited species $n^*$ is estimated using the TI-radiance measurement and equation (3). Under the assumption that most of the emitted photons are in the $2PN_2$ band, $n^*$ is an estimation of the density of the $N_2(C^3Π_u)$ excited state, in which case the quenching density $N_q$ is $2.93 \times 10^{17}$ cm$^{-3}$.

In figure 5 we plot $n^*$ as a function of the reduced diameter $pd$.

Our first observation in this plot is that the correlation of $n^*$ with diameter is weak. It appears that in the streamers in this experiment the density of excited species does not change significantly with streamer width. Our estimation of the mean $n^*$ is $(2.4 \pm 0.9) \times 10^{11}$ cm$^{-3}$ at 100 mbar, $(6.3 \pm 2.4) \times 10^{11}$ cm$^{-3}$ at 200 mbar, and $(27 \pm 9) \times 10^{11}$ cm$^{-3}$ at 400 mbar, where the errors are the standard deviation of the average value, typically near 40%. It should be noted that $n^* = 4nL/Qd$ and $pd$ are not independently measured variables, while $L$ and $pd$ are.

In figure 5 it is apparent that when pressure (i.e. neutral density) is higher, the density of excited molecules $n^*$ is larger. The density of excited species and electrons in the streamer head should scale as the square of the neutral density, $N_2$. Next we estimate the reduced density of excited species, $n^* \propto (p/p_0)^{-2}$, where $p$ is the pressure and $p_0 = 1000$ mbar is a reference pressure. With this scaling the reduced density should be independent of pressure. We plot the averaged reduced density versus pressure in figure 6, where the error bars represent one standard deviation of the averaged values. It appears that within statistical uncertainty the average reduced density is independent of pressure. The measurement at 100 mbar is higher by a factor 1.5, though it agrees with higher pressure measurements within the standard deviation margin. The reduced density at 200 and 400 mbar is $(1.6 \pm 0.6) \times 10^{13}$ cm$^{-3}$ and at 100 mbar it is $(2.4 \pm 0.9) \times 10^{13}$ cm$^{-3}$. The average of the reduced density of excited molecules ($N_2(C^3Π_u)$) over the three pressures is estimated as $(2 \pm 1) \times 10^{13}$ cm$^{-3}$. This is the expected excitation density at 1 bar.

In the introduction we described previous numerical and experimental estimations of the absolute density of electrons, $N_2(C^3Π_u)$, $N_2(A^3Σ^+_g)$ and other species. Model estimations at 1 bar are $10^{13}$–$10^{14}$ cm$^{-3}$. The experimental estimations at 1 bar range from $4 \times 10^{13}$ cm$^{-3}$ [16] and up to $9 \times 10^{14}$ cm$^{-3}$ [18]. Our estimation of the absolute reduced density is well within the range of previously reported values.

5. Discussion

Streamers can be regarded as self-organizing structures, which can be characterized by a few macroscopic parameters. Previous theoretical and experimental work has shown that when parameters such as the neutral density, the velocity, the diameter and the applied voltage are properly scaled, the physical process is essentially the same. This discussion leads to a search of other key characteristics that can be quantified. Numerical models consistently indicate that at standard and typical conditions the streamers have a reduced density $n^* = 4nL/Qd$ that is independent of pressure. The calculations predict that the reduced density $n^*$ at 1 bar is $(2 \pm 1) \times 10^{13}$ cm$^{-3}$. This is in good agreement with the experimental results.
pressure, the densities of electrons, and of other products of the passage of the streamer are on the order of $10^{13}-10^{14}$ cm$^{-3}$. These findings where confirmed by experimental work. However a rigorous examination of the density of electrons produced by the passing streamer head should be proportional to the square of the neutral density $N^2$.

We estimate the density of the $\text{N}_2(\text{C}_3\Pi_u)$ excited state at three different pressures (100, 200 and 400 mbar), and find it is consistent with $N^2$ scaling. Following this scaling, our estimation of the excitation density at 1 bar is $(2 \pm 1) \times 10^{13}$ cm$^{-3}$. This value is consistent with theoretical and experimental findings at standard pressure. We estimated the time integrated radiance of the streamers as a function of their reduced diameters, $pd$. We expected a linear trend, following equation (2).

Our results suggest that the time integrated radiance is proportional to $(pd)^{\alpha}$, with $\alpha = 0.69 \pm 0.07$ at pressures 100 and 200 mbar, and $\alpha = 0.85 \pm 0.11$ at 400 mbar. Moreover, when the time integrated radiance is plotted against the reduced diameter $pd$, the data points of all three pressures coincide (figure 4(a)). In other words, the trend at different pressures and similar conditions (similar diameters) is similar, a clear signature of scaling relations. We recall here that while the absolute radiance is measured with an error of 30%, the relative radiance is accurate to within 5% (see appendix A for details). Therefore the statistical distribution observed in the data points is most likely due to differences in the observed streamers, and to some extent, the overestimated diameters of out-of-focus streamers.

It is puzzling that the dependence on $pd$ is not linear (i.e. $\alpha < 1$). We suggest that this is an artifact of the measurement, explained by the overestimation of some streamer diameters when they are out of focus. Out-of-focus streamers can be distinguished from focused streamers only if they are significantly wider than focused streamers in the image. This happens for at least some of the streamers imaged at 400 mbar. This puzzle can be better answered experimentally if the focus artifact is resolved, for example by observing streamers in sprites [9, 46, 47], by using stereo-photographic imaging [48] to determine the 3D position of streamers and thereby their distance to the focal plane, or with guided streamers, where the trajectory of the streamer is determined by the setup [20, 49].

Alternative explanations would be related to the physics of the discharge. Streamers are optically thin, and the quenching factor Q is not related to diameter; therefore the measurements may suggest that $n^*$ is lower for thicker streamers. Is it possible that the production of excited nitrogen molecules is lower in thicker streamers? According to Naidis [23] and Li et al [34] the densities depend on the electric field, with higher fields leading to higher production of excited molecules (equation (1)). However, the densities predicted by this model in the range of fields relevant to streamer heads [8] are not very sensitive to the electric field, changing by a factor 4 at most, as was shown in figure 1. Our results suggest that the variability of the excitation density in streamer heads may be on a similar scale. The variability of the excitation density may depend on the stochastic nature of the discharge and on local conditions, and should be explored further.

6. Conclusions

We presented the results of an experimental investigation of the scaling of the time-integrated radiance of streamers, and the densities of the excited molecules responsible for these emissions. We studied streamer discharges in artificial air, in the pressure range of 100–400 mbar. Our results suggest that the time-integrated radiance, defined as the number of photons per unit area per solid angle emitted from a streamer head, depends linearly on the diameter of the streamer. Based on this finding we estimate the density of excited species in the streamer head. We find that this density depends very weakly on the streamer diameter, whereas streamers may have a slightly lower excitation density. This downward trend may be explained by the fact that at least part of the imaged streamers are not in focus.

Interestingly, we find that the radiance and the density of excited molecules exhibit similar trends at different pressures when examined under similar conditions, i.e. when plotted as a function of the reduced diameter $pd$. This is a clear indication of a scaling relation. As we showed, the average density of the molecules excited by the passage of a streamer depends only weakly on the streamer diameter. Therefore we estimated the mean densities of $\text{N}_2(\text{C}_3\Pi_u)$ at the available pressures, and the mean reduced density $n^* \times (p/p_0)^{-\alpha} = (2 \pm 1) \times 10^{13}$ cm$^{-3}$, where $p_0 = 1$bar. We show that within statistical uncertainty, this excitation density scales as the square of the neutral density.

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Appendix A. Description of camera calibration

The streamers in our setup are imaged using a Stanford Computer Optics 4QuickE intensified CCD camera, with nanosecond exposure time, mounted with a UV-Nikkor 105 mm lens, sensitive to wavelengths in the range 120–850 nm. The imaging setup was calibrated using a tungsten ribbon lamp. After initial calibration, the radiance of streamers is retrieved from the grey level measured in the ICCD camera. For that purpose the transmittance functions of the quartz and fine wire mesh windows are taken into account. The calibration procedure is described below.

The spectral photon radiance of the tungsten ribbon lamp, \( P(\lambda) \), (in photons per solid angle per unit area per second per unit wavelength) is supplied with the lamp. The signal is affected by the response function of the image intensifier in the camera, which depends on the wavelength. The gray level \((GL)\) of an illuminated pixel is therefore

\[
GL = GL_0 + K \cdot f(V_{gain}) \cdot \Omega_{IFOV} \cdot A_{opt} \cdot \Delta t \cdot \int P(\lambda) \cdot R(\lambda) \, d\lambda
\]

where \(GL_0\) is the background grey level, \(K\) is the calibration constant, \(f(V_{gain})\) represents the dependency on the intensifier gain voltage, which is controlled externally by the user, \(\Delta t\) is the exposure time, \(\Omega_{IFOV}\) is the instantaneous field of view of a pixel and \(A_{opt}\) is the effective collecting area of the lens. The spectral response of the camera is given by \(R(\lambda)\), the product of the quantum efficiency of the image intensifier and the transmittance of the UV-Nikkor lens. The quantum efficiency curve is supplied by the manufacturer with an estimated accuracy of 25%, and the transmission of the lens was measured with an accuracy of 20%. The output of this step is the calibration constant \(K\). Its absolute value has an error of ~30%. The gain voltage dependence was estimated separately as \(f(V_{gain}) = \exp(aV_{gain} + b)\), where \(a = 1.4 \cdot 10^{-2} \text{V}^{-1}\) and \(b = -6.6\), with 5% accuracy. The relative radiance measurement does not depend on the absolute value of \(K\), and its accuracy is determined by the accuracy of the gain function \(f(V_{gain})\) and the throughput \(A_{opt} \cdot \Omega_{IFOV}\). This reflects on the accuracy of the correlations we find in our results.

In the 4QuickE ICCD camera the image is formed on a photocathode which intensifies the signal, but also increases the noise. As a result, images less than 10 pixels wide are not well resolved. Each of the 1360 × 1024 CCD pixels is represented by an effective pixel of width \(d_{px} = 10.575 \mu\text{m}\) on the photo-cathode. The IFOV angle is defined as \(\Omega_{IFOV} = (d_{px} / u)^2\), where \(u\) is the distance between the image on the photocathode and the effective lens that substitutes the UV-Nikkor lens, such that the lens equation is satisfied.

The strength of the signal produced by the imaged streamers depends on the response function of the camera \(R(\lambda)\), the transmittance of the viewing window \(W(\lambda)\), and on the normalized spectral distribution of the incoming light \(S(\lambda)\). Westimated \(S(\lambda)\) by measuring the spectrum of a streamer and glow discharge at low pressures (50–200 mbar, figure A.1). The spectrum was recorded using three small Ocean Optics spectrometers together spanning the wavelength range of 230–940 nm, at several pressures and voltages, similarly to Dubrovin et al [50]. This spectrum is similar to measured and calculated sprite and streamer spectra (see e.g. [10, 51]). Streamers propagating in air radiate predominantly in the blue and the near UV second positive system (2PN2), in the wavelength range of 300–400 nm. The red first positive system (1PN2), dominant in ground sprite observations, is quenched at pressures above 1 mbar [35, 52].

The time-integrated radiance \(L_t = L \cdot \Delta t\) is determined by:
where $S(\lambda)$ is the spectral distribution of the incoming light (black curve in figure A.1) and $K$ and $f(V_{\text{gain}}) \cdot A_{\text{opt}}$ are the calibration constant and gain function determined by the calibration procedure described above. The integration boundaries are determined by the limits of the response function $R(\lambda)$. The 2PN$_2$ band is well within the sensitivity range of the camera. The uncertainty in integration boundaries leads to an error of ~2%. The TI-radiance in this expression leads to an error of ~2%. The TTL-radiance is measured in photons per solid angle per unit area (ph str$^{-1}$ cm$^{-2}$). The spectrum of the streamers and the combined transmittance and response curve $R(\lambda) \cdot W(\lambda)$ are plotted in figure A.1.

References


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