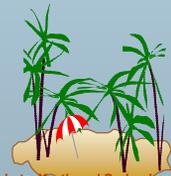




Chapter 3: Relational Model

- Structure of Relational Databases
- Relational Algebra
- Tuple Relational Calculus
- Domain Relational Calculus
- Extended Relational-Algebra-Operations
- Modification of the Database
- Views



Example of a Relation

| <i>account-number</i> | <i>branch-name</i> | <i>balance</i> |
|-----------------------|--------------------|----------------|
| A-101 | Downtown | 500 |
| A-102 | Perryridge | 400 |
| A-201 | Brighton | 900 |
| A-215 | Mianus | 700 |
| A-217 | Brighton | 750 |
| A-222 | Redwood | 700 |
| A-305 | Round Hill | 350 |





Basic Structure

- Formally, given sets D_1, D_2, \dots, D_n a **relation** r is a subset of $D_1 \times D_2 \times \dots \times D_n$
Thus a relation is a set of n-tuples (a_1, a_2, \dots, a_n) where each $a_i \in D_i$
- Example: if

$customer-name = \{Jones, Smith, Curry, Lindsay\}$

$customer-street = \{Main, North, Park\}$

$customer-city = \{Harrison, Rye, Pittsfield\}$

Then $r = \{$ (Jones, Main, Harrison),
(Smith, North, Rye),
(Curry, North, Rye),
(Lindsay, Park, Pittsfield) $\}$

is a relation over $customer-name \times customer-street \times customer-city$



Attribute Types

- Each attribute of a relation has a name
- The set of allowed values for each attribute is called the **domain** of the attribute
- Attribute values are (normally) required to be **atomic**, that is, indivisible
 - E.g. multivalued attribute values are not atomic
 - E.g. composite attribute values are not atomic
- The special value *null* is a member of every domain
- The null value causes complications in the definition of many operations
 - we shall ignore the effect of null values in our main presentation and consider their effect later





Relation Schema

- A_1, A_2, \dots, A_n are *attributes*
- $R = (A_1, A_2, \dots, A_n)$ is a *relation schema*
E.g. *Customer-schema* =
(*customer-name, customer-street, customer-city*)
- $r(R)$ is a *relation* on the *relation schema* R
E.g. *customer* (*Customer-schema*)



Relation Instance

- The current values (*relation instance*) of a relation are specified by a table
- An element t of r is a *tuple*, represented by a *row* in a table

| <i>customer-name</i> | <i>customer-street</i> | <i>customer-city</i> |
|----------------------|------------------------|----------------------|
| <i>Jones</i> | <i>Main</i> | <i>Harrison</i> |
| <i>Smith</i> | <i>North</i> | <i>Rye</i> |
| <i>Curry</i> | <i>North</i> | <i>Rye</i> |
| <i>Lindsay</i> | <i>Park</i> | <i>Pittsfield</i> |

customer

attributes (or columns)

tuples (or rows)

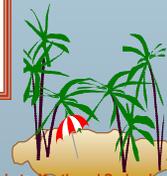




Relations are Unordered

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
- E.g. *account* relation with unordered tuples

| <i>account-number</i> | <i>branch-name</i> | <i>balance</i> |
|-----------------------|--------------------|----------------|
| A-101 | Downtown | 500 |
| A-215 | Mianus | 700 |
| A-102 | Perryridge | 400 |
| A-305 | Round Hill | 350 |
| A-201 | Brighton | 900 |
| A-222 | Redwood | 700 |
| A-217 | Brighton | 750 |



Database

- A database consists of multiple relations
- Information about an enterprise is broken up into parts, with each relation storing one part of the information

E.g.: *account* : stores information about accounts
depositor : stores information about which customer owns which account
customer : stores information about customers

- Storing all information as a single relation such as
bank(account-number, balance, customer-name, ..)
results in
 - 📌 repetition of information (e.g. two customers own an account)
 - 📌 the need for null values (e.g. represent a customer without an account)
- Normalization theory (Chapter 7) deals with how to design relational schemas





The *customer* Relation

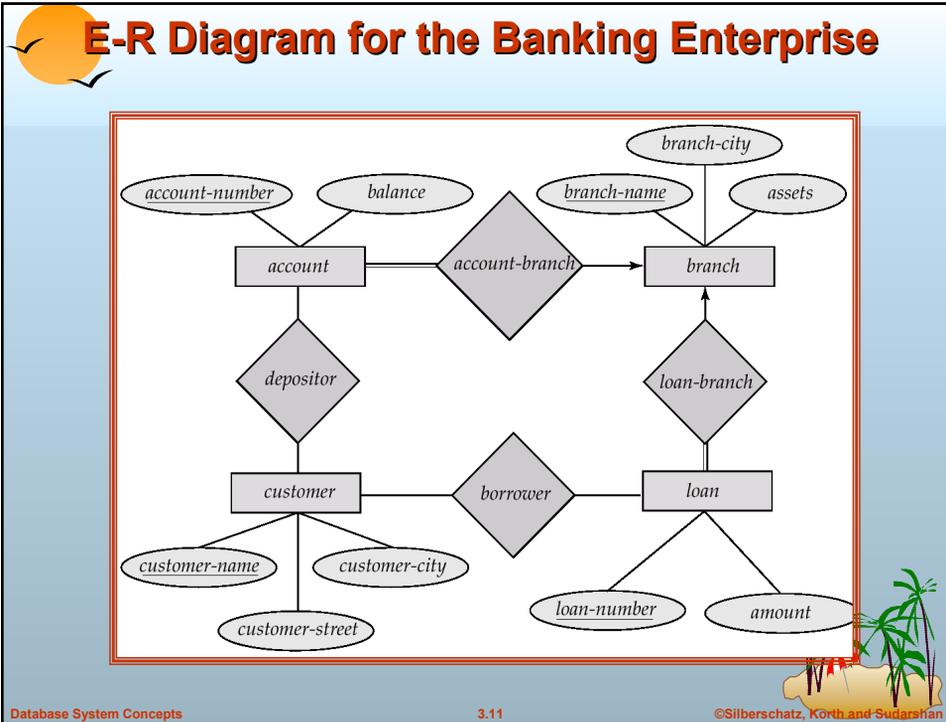
| <i>customer-name</i> | <i>customer-street</i> | <i>customer-city</i> |
|----------------------|------------------------|----------------------|
| Adams | Spring | Pittsfield |
| Brooks | Senator | Brooklyn |
| Curry | North | Rye |
| Glenn | Sand Hill | Woodside |
| Green | Walnut | Stamford |
| Hayes | Main | Harrison |
| Johnson | Alma | Palo Alto |
| Jones | Main | Harrison |
| Lindsay | Park | Pittsfield |
| Smith | North | Rye |
| Turner | Putnam | Stamford |
| Williams | Nassau | Princeton |



The *depositor* Relation

| <i>customer-name</i> | <i>account-number</i> |
|----------------------|-----------------------|
| Hayes | A-102 |
| Johnson | A-101 |
| Johnson | A-201 |
| Jones | A-217 |
| Lindsay | A-222 |
| Smith | A-215 |
| Turner | A-305 |





Keys

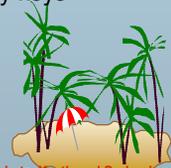
- Let $K \subseteq R$
- K is a **superkey** of R if values for K are sufficient to identify a unique tuple of each possible relation $r(R)$
 - 🔑 by “possible r ” we mean a relation r that could exist in the enterprise we are modeling.
 - 🔑 Example: $\{customer\text{-name}, customer\text{-street}\}$ and $\{customer\text{-name}\}$ are both superkeys of *Customer*, if no two customers can possibly have the same name.
- K is a **candidate key** if K is minimal
 - Example: $\{customer\text{-name}\}$ is a candidate key for *Customer*, since it is a superkey (assuming no two customers can possibly have the same name), and no subset of it is a superkey.

Database System Concepts 3.12 ©Silberschatz, Korth and Sudarshan

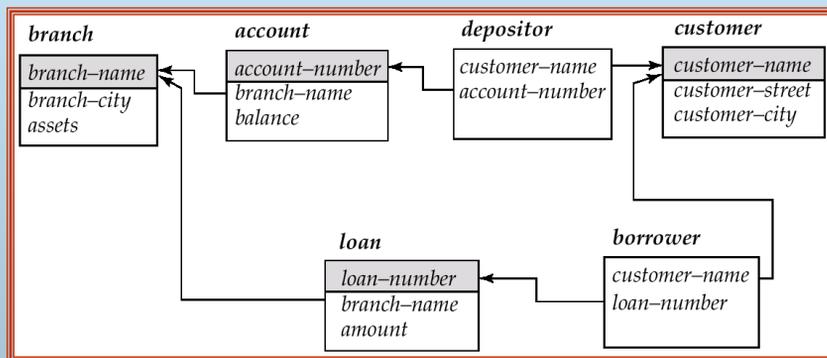


Determining Keys from E-R Sets

- **Strong entity set.** The primary key of the entity set becomes the primary key of the relation.
- **Weak entity set.** The primary key of the relation consists of the union of the primary key of the strong entity set and the discriminator of the weak entity set.
- **Relationship set.** The union of the primary keys of the related entity sets becomes a super key of the relation.
 - 📌 For binary many-to-one relationship sets, the primary key of the “many” entity set becomes the relation’s primary key.
 - 📌 For one-to-one relationship sets, the relation’s primary key can be that of either entity set.
 - 📌 For many-to-many relationship sets, the union of the primary keys becomes the relation’s primary key



Schema Diagram for the Banking Enterprise





Query Languages

- Language in which user requests information from the database.
- Categories of languages
 - ↳ procedural
 - ↳ non-procedural
- “Pure” languages:
 - ↳ Relational Algebra
 - ↳ Tuple Relational Calculus
 - ↳ Domain Relational Calculus
- Pure languages form underlying basis of query languages that people use.



Relational Algebra

- Procedural language
- Six basic operators
 - ↳ select
 - ↳ project
 - ↳ union
 - ↳ set difference
 - ↳ Cartesian product
 - ↳ rename
- The operators take two or more relations as inputs and give a new relation as a result.





Select Operation – Example

- Relation r

| A | B | C | D |
|----------|----------|----|----|
| α | α | 1 | 7 |
| α | β | 5 | 7 |
| β | β | 12 | 3 |
| β | β | 23 | 10 |

- $\sigma_{A=B \wedge D > 5}(r)$

| A | B | C | D |
|----------|----------|----|----|
| α | α | 1 | 7 |
| β | β | 23 | 10 |



Select Operation

- Notation: $\sigma_p(r)$
- p is called the **selection predicate**
- Defined as:

$$\sigma_p(r) = \{t \mid t \in r \text{ and } p(t)\}$$

Where p is a formula in propositional calculus consisting of **terms** connected by : \wedge (**and**), \vee (**or**), \neg (**not**)

Each **term** is one of:

$\langle \text{attribute} \rangle \text{ op } \langle \text{attribute} \rangle$ or $\langle \text{constant} \rangle$

where op is one of: $=, \neq, >, \geq, <, \leq$

- Example of selection:

$$\sigma_{\text{branch-name}=\text{"Perryridge"}(\text{account})}$$





Project Operation – Example

- Relation r :

| A | B | C |
|----------|----|---|
| α | 10 | 1 |
| α | 20 | 1 |
| β | 30 | 1 |
| β | 40 | 2 |

- $\Pi_{A,C}(r)$

| A | C |
|----------|---|
| α | 1 |
| α | 1 |
| β | 1 |
| β | 2 |

=

| A | C |
|----------|---|
| α | 1 |
| β | 1 |
| β | 2 |



Project Operation

- Notation:

$$\Pi_{A_1, A_2, \dots, A_k}(r)$$

where A_1, A_2 are attribute names and r is a relation name.

- The result is defined as the relation of k columns obtained by erasing the columns that are not listed
- Duplicate rows removed from result, since relations are sets
- E.g. To eliminate the *branch-name* attribute of *account*

$$\Pi_{\text{account-number}, \text{balance}}(\text{account})$$





Union Operation – Example

- Relations r, s :

| A | B |
|----------|---|
| α | 1 |
| α | 2 |
| β | 1 |

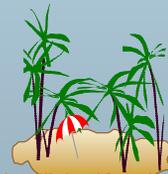
r

| A | B |
|----------|---|
| α | 2 |
| β | 3 |

s

$r \cup s$:

| A | B |
|----------|---|
| α | 1 |
| α | 2 |
| β | 1 |
| β | 3 |



Union Operation

- Notation: $r \cup s$
- Defined as:

$$r \cup s = \{t \mid t \in r \text{ or } t \in s\}$$

- For $r \cup s$ to be valid.
 - r, s must have the *same arity* (same number of attributes)
 - The attribute domains must be *compatible* (e.g., 2nd column of r deals with the same type of values as does the 2nd column of s)
- E.g. to find all customers with either an account or a loan

$$\Pi_{customer-name}(depositor) \cup \Pi_{customer-name}(borrower)$$





Set Difference Operation – Example

- Relations r, s :

| A | B |
|----------|---|
| α | 1 |
| α | 2 |
| β | 1 |

r

| A | B |
|----------|---|
| α | 2 |
| β | 3 |

s

$r - s$:

| A | B |
|----------|---|
| α | 1 |
| β | 1 |



Set Difference Operation

- Notation $r - s$
- Defined as:
$$r - s = \{t \mid t \in r \text{ and } t \notin s\}$$
- Set differences must be taken between *compatible* relations.
 - r and s must have the *same arity*
 - attribute domains of r and s must be compatible





Cartesian-Product Operation-Example

Relations r, s :

| A | B |
|----------|---|
| α | 1 |
| β | 2 |

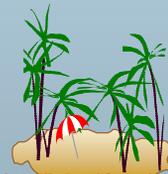
r

| C | D | E |
|----------|----|---|
| α | 10 | a |
| β | 10 | a |
| β | 20 | b |
| γ | 10 | b |

s

$r \times s$:

| A | B | C | D | E |
|----------|---|----------|----|---|
| α | 1 | α | 10 | a |
| α | 1 | β | 10 | a |
| α | 1 | β | 20 | b |
| α | 1 | γ | 10 | b |
| β | 2 | α | 10 | a |
| β | 2 | β | 10 | a |
| β | 2 | β | 20 | b |
| β | 2 | γ | 10 | b |



Cartesian-Product Operation

- Notation $r \times s$
- Defined as:

$$r \times s = \{tq \mid t \in r \text{ and } q \in s\}$$
- Assume that attributes of $r(R)$ and $s(S)$ are disjoint. (That is, $R \cap S = \emptyset$).
- If attributes of $r(R)$ and $s(S)$ are not disjoint, then renaming must be used.





Composition of Operations

- Can build expressions using multiple operations

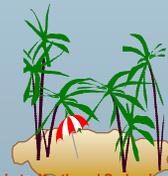
- Example: $\sigma_{A=C}(r \times s)$

- $r \times s$

| A | B | C | D | E |
|----------|---|----------|----|---|
| α | 1 | α | 10 | a |
| α | 1 | β | 10 | a |
| α | 1 | β | 20 | b |
| α | 1 | γ | 10 | b |
| β | 2 | α | 10 | a |
| β | 2 | β | 10 | a |
| β | 2 | β | 20 | b |
| β | 2 | γ | 10 | b |

- $\sigma_{A=C}(r \times s)$

| A | B | C | D | E |
|----------|---|----------|----|---|
| α | 1 | α | 10 | a |
| β | 2 | β | 20 | a |
| β | 2 | β | 20 | b |



Rename Operation

- Allows us to name, and therefore to refer to, the results of relational-algebra expressions.

- Allows us to refer to a relation by more than one name.

Example:

$$\rho_X(E)$$

returns the expression E under the name X

If a relational-algebra expression E has arity n , then

$$\rho_X(A_1, A_2, \dots, A_n)(E)$$

returns the result of expression E under the name X , and with the attributes renamed to A_1, A_2, \dots, A_n .





Banking Example

branch (branch-name, branch-city, assets)

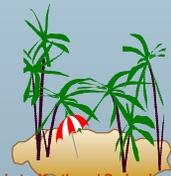
customer (customer-name, customer-street, customer-only)

account (account-number, branch-name, balance)

loan (loan-number, branch-name, amount)

depositor (customer-name, account-number)

borrower (customer-name, loan-number)



Example Queries

- Find all loans of over \$1200

$\sigma_{amount > 1200} (loan)$

- Find the loan number for each loan of an amount greater than \$1200

$\Pi_{loan-number} (\sigma_{amount > 1200} (loan))$





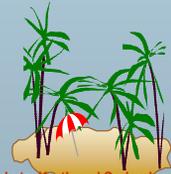
Example Queries

- Find the names of all customers who have a loan, an account, or both, from the bank

$$\Pi_{customer-name}(borrower) \cup \Pi_{customer-name}(depositor)$$

- Find the names of all customers who have a loan and an account at bank.

$$\Pi_{customer-name}(borrower) \cap \Pi_{customer-name}(depositor)$$



Example Queries

- Find the names of all customers who have a loan at the Perryridge branch.

$$\Pi_{customer-name}(\sigma_{branch-name="Perryridge"}(\sigma_{borrower.loan-number = loan.loan-number}(borrower \times loan)))$$

- Find the names of all customers who have a loan at the Perryridge branch but do not have an account at any branch of the bank.

$$\Pi_{customer-name}(\sigma_{branch-name="Perryridge"}(\sigma_{borrower.loan-number = loan.loan-number}(borrower \times loan))) - \Pi_{customer-name}(depositor)$$





Example Queries

- Find the names of all customers who have a loan at the Perryridge branch.

– Query 1

$$\Pi_{\text{customer-name}}(\sigma_{\text{branch-name} = \text{"Perryridge"}} (\sigma_{\text{borrower.loan-number} = \text{loan.loan-number}}(\text{borrower} \times \text{loan})))$$

– Query 2

$$\Pi_{\text{customer-name}}(\sigma_{\text{loan.loan-number} = \text{borrower.loan-number}} (\sigma_{\text{branch-name} = \text{"Perryridge"}}(\text{loan})) \times \text{borrower})$$



Example Queries

Find the largest account balance

- Rename *account* relation as *d*
- The query is:

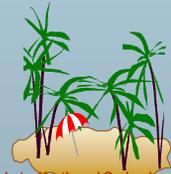
$$\Pi_{\text{balance}}(\text{account}) - \Pi_{\text{account.balance}} (\sigma_{\text{account.balance} < d.\text{balance}} (\text{account} \times \rho_d(\text{account})))$$





Formal Definition

- A basic expression in the relational algebra consists of either one of the following:
 - 📌 A relation in the database
 - 📌 A constant relation
- Let E_1 and E_2 be relational-algebra expressions; the following are all relational-algebra expressions:
 - 📌 $E_1 \cup E_2$
 - 📌 $E_1 - E_2$
 - 📌 $E_1 \times E_2$
 - 📌 $\sigma_p(E_1)$, P is a predicate on attributes in E_1
 - 📌 $\Pi_S(E_1)$, S is a list consisting of some of the attributes in E_1
 - 📌 $\rho_x(E_1)$, x is the new name for the result of E_1



Additional Operations

We define additional operations that do not add any power to the relational algebra, but that simplify common queries.

- Set intersection
- Natural join
- Division
- Assignment





Set-Intersection Operation

- Notation: $r \cap s$
- Defined as:
 - $r \cap s = \{t \mid t \in r \text{ and } t \in s\}$
- Assume:
 - 🔑 r, s have the *same arity*
 - 🔑 attributes of r and s are compatible
- Note: $r \cap s = r - (r - s)$



Set-Intersection Operation - Example

- Relation r, s :

| A | B |
|----------|---|
| α | 1 |
| α | 2 |
| β | 1 |

r

| A | B |
|----------|---|
| α | 2 |
| β | 3 |

s

- $r \cap s$

| A | B |
|----------|---|
| α | 2 |





Natural-Join Operation

- Notation: $r \bowtie s$
- Let r and s be relations on schemas R and S respectively. Then, $r \bowtie s$ is a relation on schema $R \cup S$ obtained as follows:
 - 📌 Consider each pair of tuples t_r from r and t_s from s .
 - 📌 If t_r and t_s have the same value on each of the attributes in $R \cap S$, add a tuple t to the result, where
 - 📖 t has the same value as t_r on r
 - 📖 t has the same value as t_s on s

■ Example:

$R = (A, B, C, D)$

$S = (E, B, D)$

📌 Result schema = (A, B, C, D, E)

📌 $r \bowtie s$ is defined as:

$$\Pi_{r.A, r.B, r.C, r.D, s.E} (\sigma_{r.B = s.B \wedge r.D = s.D} (r \times s))$$



Natural Join Operation – Example

■ Relations r , s :

| A | B | C | D |
|----------|---|----------|---|
| α | 1 | α | a |
| β | 2 | γ | a |
| γ | 4 | β | b |
| α | 1 | γ | a |
| δ | 2 | β | b |

r

| B | D | E |
|---|---|------------|
| 1 | a | α |
| 3 | a | β |
| 1 | a | γ |
| 2 | b | δ |
| 3 | b | ϵ |

s

$r \bowtie s$

| A | B | C | D | E |
|----------|---|----------|---|----------|
| α | 1 | α | a | α |
| α | 1 | α | a | γ |
| α | 1 | γ | a | α |
| α | 1 | γ | a | γ |
| δ | 2 | β | b | δ |





Division Operation

$$r \div s$$

- Suited to queries that include the phrase “for all”.
- Let r and s be relations on schemas R and S respectively where

$$R = (A_1, \dots, A_m, B_1, \dots, B_n)$$

$$S = (B_1, \dots, B_n)$$

The result of $r \div s$ is a relation on schema

$$R - S = (A_1, \dots, A_m)$$

$$r \div s = \{t \mid t \in \Pi_{R-S}(r) \wedge \forall u \in s (tu \in r)\}$$



Division Operation – Example

Relations r, s :

| A | B |
|------------|---|
| α | 1 |
| α | 2 |
| α | 3 |
| β | 1 |
| γ | 1 |
| δ | 1 |
| δ | 3 |
| δ | 4 |
| ϵ | 6 |
| ϵ | 1 |
| β | 2 |

| B |
|---|
| 1 |
| 2 |

s

$r \div s$:

| A |
|----------|
| α |
| β |

r





Another Division Example

Relations r, s :

| A | B | C | D | E |
|----------|---|----------|---|---|
| α | a | α | a | 1 |
| α | a | γ | a | 1 |
| α | a | γ | b | 1 |
| β | a | γ | a | 1 |
| β | a | γ | b | 3 |
| γ | a | γ | a | 1 |
| γ | a | γ | b | 1 |
| γ | a | β | b | 1 |

r

| D | E |
|---|---|
| a | 1 |
| b | 1 |

s

$r \div s$:

| A | B | C |
|----------|---|----------|
| α | a | γ |
| γ | a | γ |



Division Operation (Cont.)

Property

Let $q - r \div s$

Then q is the largest relation satisfying $q \times s \subseteq r$

Definition in terms of the basic algebra operation

Let $r(R)$ and $s(S)$ be relations, and let $S \subseteq R$

$$r \div s = \Pi_{R-S}(r) - \Pi_{R-S}((\Pi_{R-S}(r) \times s) - \Pi_{R-S,S}(r))$$

To see why

$\Pi_{R-S,S}(r)$ simply reorders attributes of r

$\Pi_{R-S}(\Pi_{R-S}(r) \times s) - \Pi_{R-S,S}(r)$ gives those tuples t in

$\Pi_{R-S}(r)$ such that for some tuple $u \in s$, $tu \notin r$.





Assignment Operation

- The assignment operation (\leftarrow) provides a convenient way to express complex queries.
 - 📖 Write query as a sequential program consisting of
 - 📖 a series of assignments
 - 📖 followed by an expression whose value is displayed as a result of the query.
 - 📖 Assignment must always be made to a temporary relation variable.
- Example: Write $r \div s$ as

$$\begin{aligned} temp1 &\leftarrow \Pi_{R-S}(r) \\ temp2 &\leftarrow \Pi_{R-S}((temp1 \times s) - \Pi_{R-S,S}(r)) \\ result &= temp1 - temp2 \end{aligned}$$

- 📖 The result to the right of the \leftarrow is assigned to the relation variable on the left of the \leftarrow .
- 📖 May use variable in subsequent expressions.



Example Queries

- Find all customers who have an account from at least the “Downtown” and the Uptown” branches.

Query 1

$$\begin{aligned} &\Pi_{CN}(\sigma_{BN=\text{“Downtown”}}(depositor \bowtie account)) \cap \\ &\Pi_{CN}(\sigma_{BN=\text{“Uptown”}}(depositor \bowtie account)) \end{aligned}$$

where CN denotes customer-name and BN denotes branch-name.

Query 2

$$\begin{aligned} &\Pi_{customer-name, branch-name}(depositor \bowtie account) \\ &\div \rho_{temp(branch-name)}(\{\{\text{“Downtown”}\}, \{\text{“Uptown”}\}\}) \end{aligned}$$




Example Queries

- Find all customers who have an account at all branches located in Brooklyn city.

$$\begin{aligned} & \Pi_{customer-name, branch-name} (depositor \bowtie account) \\ & \div \Pi_{branch-name} (\sigma_{branch-city = \text{"Brooklyn"}} (branch)) \end{aligned}$$



Extended Relational-Algebra-Operations

- Generalized Projection
- Outer Join
- Aggregate Functions





Generalized Projection

- Extends the projection operation by allowing arithmetic functions to be used in the projection list.

$$\Pi_{F_1, F_2, \dots, F_n}(E)$$

- E is any relational-algebra expression
- Each of F_1, F_2, \dots, F_n are arithmetic expressions involving constants and attributes in the schema of E .
- Given relation $credit-info(customer-name, limit, credit-balance)$, find how much more each person can spend:

$$\Pi_{customer-name, limit - credit-balance}(credit-info)$$



Aggregate Functions and Operations

- **Aggregation function** takes a collection of values and returns a single value as a result.

avg: average value

min: minimum value

max: maximum value

sum: sum of values

count: number of values

- **Aggregate operation** in relational algebra

$$G_1, G_2, \dots, G_n \mathcal{G}_{F_1(A_1), F_2(A_2), \dots, F_n(A_n)}(E)$$

📌 E is any relational-algebra expression

📌 G_1, G_2, \dots, G_n is a list of attributes on which to group (can be empty)

📌 Each F_i is an aggregate function

📌 Each A_j is an attribute name





Aggregate Operation – Example

- Relation r :

| A | B | C |
|----------|----------|----|
| α | α | 7 |
| α | β | 7 |
| β | β | 3 |
| β | β | 10 |

$g_{\text{sum}(c)}(r)$

| <i>sum-C</i> |
|--------------|
| 27 |



Aggregate Operation – Example

- Relation *account* grouped by *branch-name*:

| <i>branch-name</i> | <i>account-number</i> | <i>balance</i> |
|--------------------|-----------------------|----------------|
| Perryridge | A-102 | 400 |
| Perryridge | A-201 | 900 |
| Brighton | A-217 | 750 |
| Brighton | A-215 | 750 |
| Redwood | A-222 | 700 |

branch-name $g_{\text{sum}(\text{balance})}(\text{account})$

| <i>branch-name</i> | <i>balance</i> |
|--------------------|----------------|
| Perryridge | 1300 |
| Brighton | 1500 |
| Redwood | 700 |





Aggregate Functions (Cont.)

- Result of aggregation does not have a name
 - 🔑 Can use rename operation to give it a name
 - 🔑 For convenience, we permit renaming as part of aggregate operation

branch-name \mathcal{G} *sum(balance) as sum-balance (account)*



Outer Join

- An extension of the join operation that avoids loss of information.
- Computes the join and then adds tuples from one relation that does not match tuples in the other relation to the result of the join.
- Uses *null* values:
 - 🔑 *null* signifies that the value is unknown or does not exist
 - 🔑 All comparisons involving *null* are (roughly speaking) **false** by definition.
 - 📖 Will study precise meaning of comparisons with nulls later





Outer Join – Example

■ Relation *loan*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|--------------------|--------------------|---------------|
| L-170 | Downtown | 3000 |
| L-230 | Redwood | 4000 |
| L-260 | Perryridge | 1700 |

■ Relation *borrower*

| <i>customer-name</i> | <i>loan-number</i> |
|----------------------|--------------------|
| Jones | L-170 |
| Smith | L-230 |
| Hayes | L-155 |



Outer Join – Example

■ Inner Join

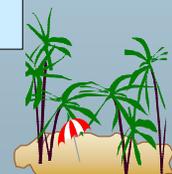
loan ⋈ *Borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |

■ Left Outer Join

loan ⋈_L *Borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-260 | Perryridge | 1700 | <i>null</i> |





Outer Join – Example

■ Right Outer Join

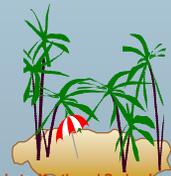
loan ⋈_r *borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-155 | <i>null</i> | <i>null</i> | Hayes |

■ Full Outer Join

loan ⋈_f *borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> | <i>customer-name</i> |
|--------------------|--------------------|---------------|----------------------|
| L-170 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-260 | Perryridge | 1700 | <i>null</i> |
| L-155 | <i>null</i> | <i>null</i> | Hayes |



Null Values

- It is possible for tuples to have a null value, denoted by *null*, for some of their attributes
- *null* signifies an unknown value or that a value does not exist.
- The result of any arithmetic expression involving *null* is *null*.
- Aggregate functions simply ignore null values
 - ☞ Is an arbitrary decision. Could have returned null as result instead.
 - ☞ We follow the semantics of SQL in its handling of null values
- For duplicate elimination and grouping, null is treated like any other value, and two nulls are assumed to be the same
 - ☞ Alternative: assume each null is different from each other
 - ☞ Both are arbitrary decisions, so we simply follow SQL





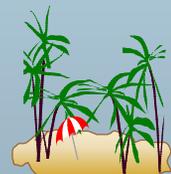
Null Values

- Comparisons with null values return the special truth value *unknown*
 - 🔑 If *false* was used instead of *unknown*, then $\text{not } (A < 5)$ would not be equivalent to $A \geq 5$
- Three-valued logic using the truth value *unknown*:
 - 🔑 OR: $(\text{unknown or true}) = \text{true}$,
 $(\text{unknown or false}) = \text{unknown}$
 $(\text{unknown or unknown}) = \text{unknown}$
 - 🔑 AND: $(\text{true and unknown}) = \text{unknown}$,
 $(\text{false and unknown}) = \text{false}$,
 $(\text{unknown and unknown}) = \text{unknown}$
 - 🔑 NOT: $(\text{not unknown}) = \text{unknown}$
 - 🔑 In SQL "*P is unknown*" evaluates to true if predicate *P* evaluates to *unknown*
- Result of select predicate is treated as *false* if it evaluates to *unknown*



Modification of the Database

- The content of the database may be modified using the following operations:
 - 🔑 Deletion
 - 🔑 Insertion
 - 🔑 Updating
- All these operations are expressed using the assignment operator.



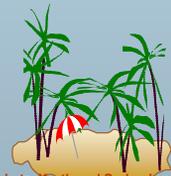


Deletion

- A delete request is expressed similarly to a query, except instead of displaying tuples to the user, the selected tuples are removed from the database.
- Can delete only whole tuples; cannot delete values on only particular attributes
- A deletion is expressed in relational algebra by:

$$r \leftarrow r - E$$

where r is a relation and E is a relational algebra query.



Deletion Examples

- Delete all account records in the Perryridge branch.

$$account \leftarrow account - \sigma_{branch-name = "Perryridge"}(account)$$

- Delete all loan records with amount in the range of 0 to 50

$$loan \leftarrow loan - \sigma_{amount \geq 0 \text{ and } amount \leq 50}(loan)$$

- Delete all accounts at branches located in Needham.

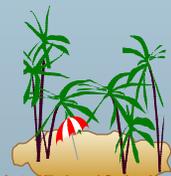
$$r_1 \leftarrow \sigma_{branch-city = "Needham"}(account \bowtie branch)$$

$$r_2 \leftarrow \Pi_{branch-name, account-number, balance}(r_1)$$

$$r_3 \leftarrow \Pi_{customer-name, account-number}(r_2 \bowtie depositor)$$

$$account \leftarrow account - r_2$$

$$depositor \leftarrow depositor - r_3$$





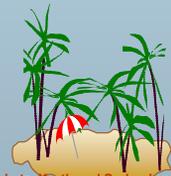
Insertion

- To insert data into a relation, we either:
 - 📌 specify a tuple to be inserted
 - 📌 write a query whose result is a set of tuples to be inserted
- in relational algebra, an insertion is expressed by:

$$r \leftarrow r \cup E$$

where r is a relation and E is a relational algebra expression.

- The insertion of a single tuple is expressed by letting E be a constant relation containing one tuple.



Insertion Examples

- Insert information in the database specifying that Smith has \$1200 in account A-973 at the Perryridge branch.

$$account \leftarrow account \cup \{("Perryridge", A-973, 1200)\}$$

$$depositor \leftarrow depositor \cup \{("Smith", A-973)\}$$

- Provide as a gift for all loan customers in the Perryridge branch, a \$200 savings account. Let the loan number serve as the account number for the new savings account.

$$r_1 \leftarrow (\sigma_{branch-name = "Perryridge"}(borrower \bowtie loan))$$

$$account \leftarrow account \cup \Pi_{branch-name, account-number, 200}(r_1)$$

$$depositor \leftarrow depositor \cup \Pi_{customer-name, loan-number}(r_1)$$





Updating

- A mechanism to change a value in a tuple without changing *all* values in the tuple
- Use the generalized projection operator to do this task

$$r \leftarrow \Pi_{F_1, F_2, \dots, F_i} (r)$$

- Each F_i is either
 - 📌 the i th attribute of r , if the i th attribute is not updated, or,
 - 📌 if the attribute is to be updated F_i is an expression, involving only constants and the attributes of r , which gives the new value for the attribute



Update Examples

- Make interest payments by increasing all balances by 5 percent.

$$account \leftarrow \Pi_{AN, BN, BAL * 1.05} (account)$$

where AN , BN and BAL stand for *account-number*, *branch-name* and *balance*, respectively.

- Pay all accounts with balances over \$10,000 6 percent interest and pay all others 5 percent

$$account \leftarrow \Pi_{AN, BN, BAL * 1.06} (\sigma_{BAL > 10000} (account)) \cup \Pi_{AN, BN, BAL * 1.05} (\sigma_{BAL \leq 10000} (account))$$



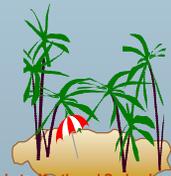


Views

- In some cases, it is not desirable for all users to see the entire logical model (i.e., all the actual relations stored in the database.)
- Consider a person who needs to know a customer's loan number but has no need to see the loan amount. This person should see a relation described, in the relational algebra, by

$$\Pi_{customer-name, loan-number}(borrower \bowtie loan)$$

- Any relation that is not of the conceptual model but is made visible to a user as a "virtual relation" is called a **view**.



View Definition

- A view is defined using the **create view** statement which has the form

create view *v* **as** <query expression>

where <query expression> is any legal relational algebra query expression. The view name is represented by *v*.

- Once a view is defined, the view name can be used to refer to the virtual relation that the view generates.
- View definition is not the same as creating a new relation by evaluating the query expression
 - 📌 Rather, a view definition causes the saving of an expression; the expression is substituted into queries using the view.





View Examples

- Consider the view (named *all-customer*) consisting of branches and their customers.

create view *all-customer* as

$$\Pi_{branch-name, customer-name} (depositor \bowtie account) \\ \cup \Pi_{branch-name, customer-name} (borrower \bowtie loan)$$

- We can find all customers of the Perryridge branch by writing:

$$\Pi_{branch-name} \\ (\sigma_{branch-name = \text{"Perryridge"}} (all-customer))$$



Updates Through View

- Database modifications expressed as views must be translated to modifications of the actual relations in the database.
- Consider the person who needs to see all loan data in the *loan* relation except *amount*. The view given to the person, *branch-loan*, is defined as:

create view *branch-loan* as

$$\Pi_{branch-name, loan-number} (loan)$$

- Since we allow a view name to appear wherever a relation name is allowed, the person may write:

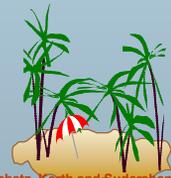
$$branch-loan \leftarrow branch-loan \cup \{(\text{"Perryridge"}, L-37)\}$$





Updates Through Views (Cont.)

- The previous insertion must be represented by an insertion into the actual relation *loan* from which the view *branch-loan* is constructed.
- An insertion into *loan* requires a value for *amount*. The insertion can be dealt with by either.
 - 🔑 rejecting the insertion and returning an error message to the user.
 - 🔑 inserting a tuple ("L-37", "Perryridge", *null*) into the *loan* relation
- Some updates through views are impossible to translate into database relation updates
 - 🔑 create view *v* as $\sigma_{branch-name = \text{"Perryridge"}}(account)$
 $v \leftarrow v \cup (L-99, \text{Downtown}, 23)$
- Others cannot be translated uniquely
 - 🔑 $all\text{-}customer \leftarrow all\text{-}customer \cup \{(\text{"Perryridge"}, \text{"John"})\}$
 - 📄 Have to choose loan or account, and create a new loan/account number!



Views Defined Using Other Views

- One view may be used in the expression defining another view
- A view relation v_1 is said to **depend directly** on a view relation v_2 if v_2 is used in the expression defining v_1
- A view relation v_1 is said to **depend on** view relation v_2 if either v_1 depends directly to v_2 or there is a path of dependencies from v_1 to v_2
- A view relation v is said to be **recursive** if it depends on itself.





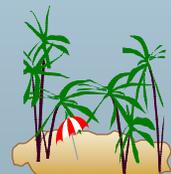
View Expansion

- A way to define the meaning of views defined in terms of other views.
- Let view v_1 be defined by an expression e_1 that may itself contain uses of view relations.
- View expansion of an expression repeats the following replacement step:
 - repeat**
 - Find any view relation v_i in e_1
 - Replace the view relation v_i by the expression defining v_i
 - until** no more view relations are present in e_1
- As long as the view definitions are not recursive, this loop will terminate



Tuple Relational Calculus

- A nonprocedural query language, where each query is of the form $\{t \mid P(t)\}$
- It is the set of all tuples t such that predicate P is true for t
- t is a *tuple variable*, $t[A]$ denotes the value of tuple t on attribute A
- $t \in r$ denotes that tuple t is in relation r
- P is a *formula* similar to that of the predicate calculus





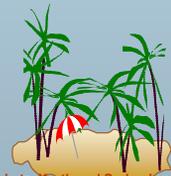
Predicate Calculus Formula

1. Set of attributes and constants
2. Set of comparison operators: (e.g., $<$, \leq , $=$, \neq , $>$, \geq)
3. Set of connectives: and (\wedge), or (\vee), not (\neg)
4. Implication (\Rightarrow): $x \Rightarrow y$, if x is true, then y is true

$$x \Rightarrow y \equiv \neg x \vee y$$

5. Set of quantifiers:

- $\exists t \in r (Q(t)) \equiv$ "there exists" a tuple t in relation r such that predicate $Q(t)$ is true
- $\forall t \in r (Q(t)) \equiv Q$ is true "for all" tuples t in relation r



Banking Example

- *branch* (*branch-name*, *branch-city*, *assets*)
- *customer* (*customer-name*, *customer-street*, *customer-city*)
- *account* (*account-number*, *branch-name*, *balance*)
- *loan* (*loan-number*, *branch-name*, *amount*)
- *depositor* (*customer-name*, *account-number*)
- *borrower* (*customer-name*, *loan-number*)





Example Queries

- Find the *loan-number*, *branch-name*, and *amount* for loans of over \$1200

$$\{t \mid t \in \text{loan} \wedge t[\text{amount}] > 1200\}$$

- Find the loan number for each loan of an amount greater than \$1200

$$\{t \mid \exists s \in \text{loan} (t[\text{loan-number}] = s[\text{loan-number}] \wedge s[\text{amount}] > 1200)\}$$

Notice that a relation on schema [*loan-number*] is implicitly defined by the query



Example Queries

- Find the names of all customers having a loan, an account, or both at the bank

$$\{t \mid \exists s \in \text{borrower} (t[\text{customer-name}] = s[\text{customer-name}]) \vee \exists u \in \text{depositor} (t[\text{customer-name}] = u[\text{customer-name}])\}$$

- Find the names of all customers who have a loan and an account at the bank

$$\{t \mid \exists s \in \text{borrower} (t[\text{customer-name}] = s[\text{customer-name}]) \wedge \exists u \in \text{depositor} (t[\text{customer-name}] = u[\text{customer-name}])\}$$





Example Queries

- Find the names of all customers having a loan at the Perryridge branch

$$\{t \mid \exists s \in \text{borrower}(t[\text{customer-name}] = s[\text{customer-name}] \\ \wedge \exists u \in \text{loan}(u[\text{branch-name}] = \text{"Perryridge"} \\ \wedge u[\text{loan-number}] = s[\text{loan-number}]))\}$$

- Find the names of all customers who have a loan at the Perryridge branch, but no account at any branch of the bank

$$\{t \mid \exists s \in \text{borrower}(t[\text{customer-name}] = s[\text{customer-name}] \\ \wedge \exists u \in \text{loan}(u[\text{branch-name}] = \text{"Perryridge"} \\ \wedge u[\text{loan-number}] = s[\text{loan-number}])) \\ \wedge \text{not } \exists v \in \text{depositor}(v[\text{customer-name}] = \\ t[\text{customer-name}])\}$$


Example Queries

- Find the names of all customers having a loan from the Perryridge branch, and the cities they live in

$$\{t \mid \exists s \in \text{loan}(s[\text{branch-name}] = \text{"Perryridge"} \\ \wedge \exists u \in \text{borrower}(u[\text{loan-number}] = s[\text{loan-number}] \\ \wedge t[\text{customer-name}] = u[\text{customer-name}]) \\ \wedge \exists v \in \text{customer}(u[\text{customer-name}] = v[\text{customer-name}] \\ \wedge t[\text{customer-city}] = v[\text{customer-city}]))\}$$




Example Queries

- Find the names of all customers who have an account at all branches located in Brooklyn:

$$\{t \mid \exists c \in \text{customer} (t[\text{customer.name}] = c[\text{customer-name}]) \wedge \\ \forall s \in \text{branch} (s[\text{branch-city}] = \text{"Brooklyn"} \Rightarrow \\ \exists u \in \text{account} (s[\text{branch-name}] = u[\text{branch-name}] \\ \wedge \exists s \in \text{depositor} (t[\text{customer-name}] = s[\text{customer-name}] \\ \wedge s[\text{account-number}] = u[\text{account-number}]))))\}$$


Safety of Expressions

- It is possible to write tuple calculus expressions that generate infinite relations.
- For example, $\{t \mid \neg t \in r\}$ results in an infinite relation if the domain of any attribute of relation r is infinite
- To guard against the problem, we restrict the set of allowable expressions to safe expressions.
- An expression $\{t \mid P(t)\}$ in the tuple relational calculus is *safe* if every component of t appears in one of the relations, tuples, or constants that appear in P

NOTE: this is more than just a syntax condition.

E.g. $\{t \mid t[A]=5 \vee \text{true}\}$ is not safe --- it defines an infinite set with attribute values that do not appear in any relation or tuples or constants in P .



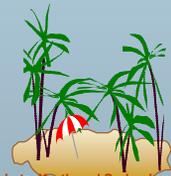


Domain Relational Calculus

- A nonprocedural query language equivalent in power to the tuple relational calculus
- Each query is an expression of the form:

$$\{ \langle x_1, x_2, \dots, x_n \rangle \mid P(x_1, x_2, \dots, x_n) \}$$

- 📌 x_1, x_2, \dots, x_n represent domain variables
- 📌 P represents a formula similar to that of the predicate calculus



Example Queries

- Find the *loan-number*, *branch-name*, and *amount* for loans of over \$1200

$$\{ \langle l, b, a \rangle \mid \langle l, b, a \rangle \in loan \wedge a > 1200 \}$$

- Find the names of all customers who have a loan of over \$1200

$$\{ \langle c \rangle \mid \exists l, b, a (\langle c, l \rangle \in borrower \wedge \langle l, b, a \rangle \in loan \wedge a > 1200) \}$$

- Find the names of all customers who have a loan from the Perryridge branch and the loan amount:

$$\{ \langle c, a \rangle \mid \exists l (\langle c, l \rangle \in borrower \wedge \exists b (\langle l, b, a \rangle \in loan \wedge b = \text{"Perryridge"})) \}$$

$$\text{or } \{ \langle c, a \rangle \mid \exists l (\langle c, l \rangle \in borrower \wedge \langle l, \text{"Perryridge"}, a \rangle \in loan) \}$$





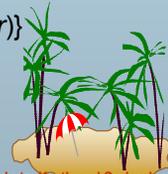
Example Queries

- Find the names of all customers having a loan, an account, or both at the Perryridge branch:

$$\{ \langle c \rangle \mid \exists l (\langle \langle c, l \rangle \in \text{borrower} \wedge \exists b, a (\langle l, b, a \rangle \in \text{loan} \wedge b = \text{"Perryridge"})) \vee \exists a (\langle c, a \rangle \in \text{depositor} \wedge \exists b, n (\langle a, b, n \rangle \in \text{account} \wedge b = \text{"Perryridge"}))) \}$$

- Find the names of all customers who have an account at all branches located in Brooklyn:

$$\{ \langle c \rangle \mid \exists s, n (\langle c, s, n \rangle \in \text{customer}) \wedge \forall x, y, z (\langle x, y, z \rangle \in \text{branch} \wedge y = \text{"Brooklyn"} \Rightarrow \exists a, b (\langle x, y, z \rangle \in \text{account} \wedge \langle c, a \rangle \in \text{depositor})) \}$$



Safety of Expressions

$$\{ \langle x_1, x_2, \dots, x_n \rangle \mid P(x_1, x_2, \dots, x_n) \}$$

is safe if all of the following hold:

- All values that appear in tuples of the expression are values from $dom(P)$ (that is, the values appear either in P or in a tuple of a relation mentioned in P).
- For every “there exists” subformula of the form $\exists x (P_1(x))$, the subformula is true if and only if there is a value of x in $dom(P_1)$ such that $P_1(x)$ is true.
- For every “for all” subformula of the form $\forall x (P_1(x))$, the subformula is true if and only if $P_1(x)$ is true for all values x from $dom(P_1)$.



End of Chapter 3



Result of $\sigma_{branch-name = \text{"Perryridge"}}$ (*loan*)

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|--------------------|--------------------|---------------|
| L-15 | Perryridge | 1500 |
| L-16 | Perryridge | 1300 |





Loan Number and the Amount of the Loan

| <i>loan-number</i> | <i>amount</i> |
|--------------------|---------------|
| L-11 | 900 |
| L-14 | 1500 |
| L-15 | 1500 |
| L-16 | 1300 |
| L-17 | 1000 |
| L-23 | 2000 |
| L-93 | 500 |



Names of All Customers Who Have Either a Loan or an Account

| <i>customer-name</i> |
|----------------------|
| Adams |
| Curry |
| Hayes |
| Jackson |
| Jones |
| Smith |
| Williams |
| Lindsay |
| Johnson |
| Turner |





Customers With An Account But No Loan

customer-name

Johnson
Lindsay
Turner



Result of *borrower* × *loan*

| <i>customer-name</i> | <i>borrower</i> <i>loan-number</i> | <i>loan</i> <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|----------------------|---------------------------------------|-----------------------------------|--------------------|---------------|
| Adams | L-16 | L-11 | Round Hill | 900 |
| Adams | L-16 | L-14 | Downtown | 1500 |
| Adams | L-16 | L-15 | Perryridge | 1500 |
| Adams | L-16 | L-16 | Perryridge | 1300 |
| Adams | L-16 | L-17 | Downtown | 1000 |
| Adams | L-16 | L-23 | Redwood | 2000 |
| Adams | L-16 | L-93 | Mianus | 500 |
| Curry | L-93 | L-11 | Round Hill | 900 |
| Curry | L-93 | L-14 | Downtown | 1500 |
| Curry | L-93 | L-15 | Perryridge | 1500 |
| Curry | L-93 | L-16 | Perryridge | 1300 |
| Curry | L-93 | L-17 | Downtown | 1000 |
| Curry | L-93 | L-23 | Redwood | 2000 |
| Curry | L-93 | L-93 | Mianus | 500 |
| Hayes | L-15 | L-11 | | 900 |
| Hayes | L-15 | L-14 | | 1500 |
| Hayes | L-15 | L-15 | | 1500 |
| Hayes | L-15 | L-16 | | 1300 |
| Hayes | L-15 | L-17 | | 1000 |
| Hayes | L-15 | L-23 | | 2000 |
| Hayes | L-15 | L-93 | | 500 |
| ... | ... | ... | ... | ... |
| ... | ... | ... | ... | ... |
| ... | ... | ... | ... | ... |
| Smith | L-23 | L-11 | Round Hill | 900 |
| Smith | L-23 | L-14 | Downtown | 1500 |
| Smith | L-23 | L-15 | Perryridge | 1500 |
| Smith | L-23 | L-16 | Perryridge | 1300 |
| Smith | L-23 | L-17 | Downtown | 1000 |
| Smith | L-23 | L-23 | Redwood | 2000 |
| Smith | L-23 | L-93 | Mianus | 500 |
| Williams | L-17 | L-11 | Round Hill | 900 |
| Williams | L-17 | L-14 | Downtown | 1500 |
| Williams | L-17 | L-15 | Perryridge | 1500 |
| Williams | L-17 | L-16 | Perryridge | 1300 |
| Williams | L-17 | L-17 | Downtown | 1000 |
| Williams | L-17 | L-23 | Redwood | 2000 |
| Williams | L-17 | L-93 | Mianus | 500 |





Result of $\sigma_{\text{branch-name} = \text{"Perryridge"}} (\text{borrower} \times \text{loan})$

| <i>customer-name</i> | <i>borrower. loan-number</i> | <i>loan. loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|----------------------|----------------------------------|------------------------------|--------------------|---------------|
| Adams | L-16 | L-15 | Perryridge | 1500 |
| Adams | L-16 | L-16 | Perryridge | 1300 |
| Curry | L-93 | L-15 | Perryridge | 1500 |
| Curry | L-93 | L-16 | Perryridge | 1300 |
| Hayes | L-15 | L-15 | Perryridge | 1500 |
| Hayes | L-15 | L-16 | Perryridge | 1300 |
| Jackson | L-14 | L-15 | Perryridge | 1500 |
| Jackson | L-14 | L-16 | Perryridge | 1300 |
| Jones | L-17 | L-15 | Perryridge | 1500 |
| Jones | L-17 | L-16 | Perryridge | 1300 |
| Smith | L-11 | L-15 | Perryridge | 1500 |
| Smith | L-11 | L-16 | Perryridge | 1300 |
| Smith | L-23 | L-15 | Perryridge | 1500 |
| Smith | L-23 | L-16 | Perryridge | 1300 |
| Williams | L-17 | L-15 | Perryridge | 1500 |
| Williams | L-17 | L-16 | Perryridge | 1300 |



Result of $\Pi_{\text{customer-name}}$

| <i>customer-name</i> |
|----------------------|
| Adams |
| Hayes |





Result of the Subexpression

| <i>balance</i> |
|----------------|
| 500 |
| 400 |
| 700 |
| 750 |
| 350 |



Largest Account Balance in the Bank

| <i>balance</i> |
|----------------|
| 900 |

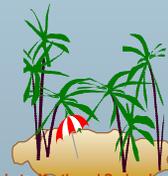




Customers Who Live on the Same Street and In the Same City as Smith

customer-name

Curry
Smith



Customers With Both an Account and a Loan at the Bank

customer-name

Hayes
Jones
Smith





**Result of $\Pi_{customer-name, loan-number, amount}$
(*borrower* \bowtie *loan*)**

| <i>customer-name</i> | <i>loan-number</i> | <i>amount</i> |
|----------------------|--------------------|---------------|
| Adams | L-16 | 1300 |
| Curry | L-93 | 500 |
| Hayes | L-15 | 1500 |
| Jackson | L-14 | 1500 |
| Jones | L-17 | 1000 |
| Smith | L-23 | 2000 |
| Smith | L-11 | 900 |
| Williams | L-17 | 1000 |



**Result of $\Pi_{branch-name}(\sigma_{customer-city =$
"Harrison")(customer \bowtie account \bowtie depositor))**

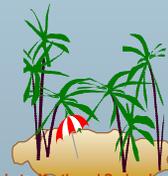
| <i>branch-name</i> |
|--------------------|
| Brighton |
| Perryridge |





Result of $\Pi_{branch-name}(\sigma_{branch-city = \text{“Brooklyn”}}(branch))$

| <i>branch-name</i> |
|--------------------|
| Brighton |
| Downtown |



Result of $\Pi_{customer-name, branch-name}(depositor \bowtie account)$

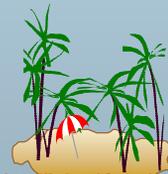
| <i>customer-name</i> | <i>branch-name</i> |
|----------------------|--------------------|
| Hayes | Perryridge |
| Johnson | Downtown |
| Johnson | Brighton |
| Jones | Brighton |
| Lindsay | Redwood |
| Smith | Mianus |
| Turner | Round Hill |





The *credit-info* Relation

| <i>customer-name</i> | <i>branch-name</i> |
|----------------------|--------------------|
| Hayes | Perryridge |
| Johnson | Downtown |
| Johnson | Brighton |
| Jones | Brighton |
| Lindsay | Redwood |
| Smith | Mianus |
| Turner | Round Hill |



Result of $\Pi_{customer-name, (limit - credit-balance)}$ as *credit-available* (***credit-info***).

| <i>customer-name</i> | <i>credit-available</i> |
|----------------------|-------------------------|
| Curry | 250 |
| Jones | 5300 |
| Smith | 1600 |
| Hayes | 0 |





The *pt-works* Relation

| <i>employee-name</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|--------------------|---------------|
| Adams | Perryridge | 1500 |
| Brown | Perryridge | 1300 |
| Gopal | Perryridge | 5300 |
| Johnson | Downtown | 1500 |
| Loreena | Downtown | 1300 |
| Peterson | Downtown | 2500 |
| Rao | Austin | 1500 |
| Sato | Austin | 1600 |



The *pt-works* Relation After Grouping

| <i>employee-name</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|--------------------|---------------|
| Rao | Austin | 1500 |
| Sato | Austin | 1600 |
| Johnson | Downtown | 1500 |
| Loreena | Downtown | 1300 |
| Peterson | Downtown | 2500 |
| Adams | Perryridge | 1500 |
| Brown | Perryridge | 1300 |
| Gopal | Perryridge | 5300 |





Result of $\text{branch-name } \zeta \text{ sum}(\text{salary})$ (pt-works)

| <i>branch-name</i> | <i>sum of salary</i> |
|--------------------|----------------------|
| Austin | 3100 |
| Downtown | 5300 |
| Perryridge | 8100 |



Result of $\text{branch-name } \zeta \text{ sum salary, max}(\text{salary}) \text{ as max-salary}$ (pt-works)

| <i>branch-name</i> | <i>sum-salary</i> | <i>max-salary</i> |
|--------------------|-------------------|-------------------|
| Austin | 3100 | 1600 |
| Downtown | 5300 | 2500 |
| Perryridge | 8100 | 5300 |

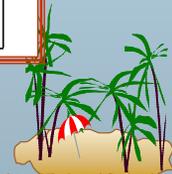




The *employee* and *ft-works* Relations

| <i>employee-name</i> | <i>street</i> | <i>city</i> |
|----------------------|---------------|--------------|
| Coyote | Toon | Hollywood |
| Rabbit | Tunnel | Carrotville |
| Smith | Revolver | Death Valley |
| Williams | Seaview | Seattle |

| <i>employee-name</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|--------------------|---------------|
| Coyote | Mesa | 1500 |
| Rabbit | Mesa | 1300 |
| Gates | Redmond | 5300 |
| Williams | Redmond | 1500 |



The Result of *employee* ⋈ *ft-works*

| <i>employee-name</i> | <i>street</i> | <i>city</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|---------------|-------------|--------------------|---------------|
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |





The Result of $\text{employee} \bowtie \text{ft-works}$

| <i>employee-name</i> | <i>street</i> | <i>city</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|---------------|--------------|--------------------|---------------|
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Smith | Revolver | Death Valley | <i>null</i> | <i>null</i> |



Result of $\text{employee} \bowtie \text{ft-works}$

| <i>employee-name</i> | <i>street</i> | <i>city</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|---------------|-------------|--------------------|---------------|
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Gates | <i>null</i> | <i>null</i> | Redmond | 5300 |





Result of employee \bowtie ft-works

| <i>employee-name</i> | <i>street</i> | <i>city</i> | <i>branch-name</i> | <i>salary</i> |
|----------------------|---------------|--------------|--------------------|---------------|
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Smith | Revolver | Death Valley | <i>null</i> | <i>null</i> |
| Gates | <i>null</i> | <i>null</i> | Redmond | 5300 |



Tuples Inserted Into *loan* and *borrower*

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|--------------------|--------------------|---------------|
| L-11 | Round Hill | 900 |
| L-14 | Downtown | 1500 |
| L-15 | Perryridge | 1500 |
| L-16 | Perryridge | 1300 |
| L-17 | Downtown | 1000 |
| L-23 | Redwood | 2000 |
| L-93 | Mianus | 500 |
| <i>null</i> | <i>null</i> | 1900 |

| <i>customer-name</i> | <i>loan-number</i> |
|----------------------|--------------------|
| Adams | L-16 |
| Curry | L-93 |
| Hayes | L-15 |
| Jackson | L-14 |
| Jones | L-17 |
| Smith | L-11 |
| Smith | L-23 |
| Williams | L-17 |
| Johnson | <i>null</i> |

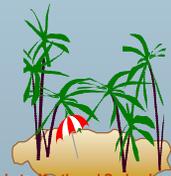




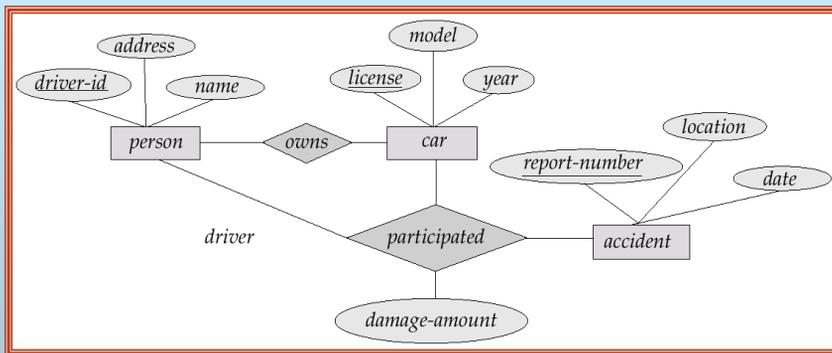
Names of All Customers Who Have a Loan at the Perryridge Branch

customer-name

Adams
Hayes



E-R Diagram





The *branch* Relation

| <i>branch-name</i> | <i>branch-city</i> | <i>assets</i> |
|--------------------|--------------------|---------------|
| Brighton | Brooklyn | 7100000 |
| Downtown | Brooklyn | 9000000 |
| Mianus | Horseneck | 400000 |
| North Town | Rye | 3700000 |
| Perryridge | Horseneck | 1700000 |
| Pownal | Bennington | 300000 |
| Redwood | Palo Alto | 2100000 |
| Round Hill | Horseneck | 8000000 |



The *loan* Relation

| <i>loan-number</i> | <i>branch-name</i> | <i>amount</i> |
|--------------------|--------------------|---------------|
| L-11 | Round Hill | 900 |
| L-14 | Downtown | 1500 |
| L-15 | Perryridge | 1500 |
| L-16 | Perryridge | 1300 |
| L-17 | Downtown | 1000 |
| L-23 | Redwood | 2000 |
| L-93 | Mianus | 500 |





The borrower Relation

| <i>customer-name</i> | <i>loan-number</i> |
|----------------------|--------------------|
| Adams | L-16 |
| Curry | L-93 |
| Hayes | L-15 |
| Jackson | L-14 |
| Jones | L-17 |
| Smith | L-11 |
| Smith | L-23 |
| Williams | L-17 |

