



Chapter 5: Other Relational Languages

- Query-by-Example (QBE)
- Datalog



Query-by-Example (QBE)

- Basic Structure
- Queries on One Relation
- Queries on Several Relations
- The Condition Box
- The Result Relation
- Ordering the Display of Tuples
- Aggregate Operations
- Modification of the Database





QBE — Basic Structure

- A graphical query language which is based (roughly) on the domain relational calculus
- Two dimensional syntax – system creates templates of relations that are requested by users
- Queries are expressed “by example”



QBE Skeleton Tables for the Bank Example

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>

<i>customer</i>	<i>customer-name</i>	<i>customer-street</i>	<i>customer-city</i>

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>





QBE Skeleton Tables (Cont.)

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>	
<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>	



Queries on One Relation

- Find all loan numbers at the Perryridge branch.

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	P. _x	Perryridge	

- _x is a variable (optional; can be omitted in above query)
- P. means print (display)
- duplicates are removed by default
- To retain duplicates use P.ALL

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	P.ALL	Perryridge	





Queries on One Relation (Cont.)

- Display full details of all loans

Method 1:

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	P._x	P._y	P._z

Method 2: Shorthand notation

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
P.			



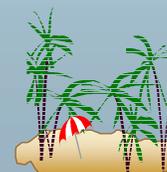
Queries on One Relation (Cont.)

- Find the loan number of all loans with a loan amount of more than \$700

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	P.		>700

- Find names of all branches that are not located in Brooklyn

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	P.	¬ Brooklyn	





Queries on One Relation (Cont.)

- Find the loan numbers of all loans made jointly to Smith and Jones.

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
	"Smith"	P..x
	"Jones"	..x

- Find all customers who live in the same city as Jones

<i>customer</i>	<i>customer-name</i>	<i>customer-street</i>	<i>customer-city</i>
	P..x		..y
	Jones		..y

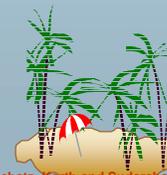


Queries on Several Relations

- Find the names of all customers who have a loan from the Perryridge branch.

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	..x	Perryridge	

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
	P..y	..x





Queries on Several Relations (Cont.)

- Find the names of all customers who have both an account and a loan at the bank.

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	P..x	

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
	..x	



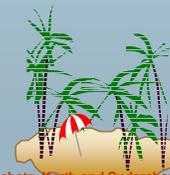
Negation in QBE

- Find the names of all customers who have an account at the bank, but do not have a loan from the bank.

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	P..x	

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
¬	..x	

¬ means "there does not exist"





Negation in QBE (Cont.)

- Find all customers who have at least two accounts.

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	P_x	$_y$
	$_x$	$\neg _y$

\neg means "not equal to"



The Condition Box

- Allows the expression of constraints on domain variables that are either inconvenient or impossible to express within the skeleton tables.
- Complex conditions can be used in condition boxes
- E.g. Find the loan numbers of all loans made to Smith, to Jones, or to both jointly

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>		
	$_n$	P_x		
<table border="1"> <thead> <tr> <th><i>conditions</i></th> </tr> </thead> <tbody> <tr> <td>$_n = \text{Smith or } _n = \text{Jones}$</td> </tr> </tbody> </table>			<i>conditions</i>	$_n = \text{Smith or } _n = \text{Jones}$
<i>conditions</i>				
$_n = \text{Smith or } _n = \text{Jones}$				





Condition Box (Cont.)

- QBE supports an interesting syntax for expressing alternative values

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	P,	_x	
<i>conditions</i>			
_x = (Brooklyn or Queens)			



Condition Box (Cont.)

- Find all account numbers with a balance between \$1,300 and \$1,500

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
	P,		_x
<i>conditions</i>			
_x ≥ 1300			
_x ≤ 1500			

- Find all account numbers with a balance between \$1,300 and \$2,000 but not exactly \$1,500.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
	P,		_x
<i>conditions</i>			
_x = (≥ 1300 and ≤ 2000 and ¬ 1500)			





Condition Box (Cont.)

- Find all branches that have assets greater than those of at least one branch located in Brooklyn

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	P..x	Brooklyn	.y .z

<i>conditions</i>
.y > .z



The Result Relation

- Find the *customer-name*, *account-number*, and *balance* for all customers who have an account at the Perryridge branch.
 - 🔑 We need to:
 - 📖 Join *depositor* and *account*.
 - 📖 Project *customer-name*, *account-number* and *balance*.
 - 🔑 To accomplish this we:
 - 📖 Create a skeleton table, called *result*, with attributes *customer-name*, *account-number*, and *balance*.
 - 📖 Write the query.





The Result Relation (Cont.)

- The resulting query is:

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
	<i>y</i>	Perryridge	<i>z</i>

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	<i>x</i>	<i>y</i>

<i>result</i>	<i>customer-name</i>	<i>account-number</i>	<i>balance</i>
P.	<i>x</i>	<i>y</i>	<i>z</i>



Ordering the Display of Tuples

- AO = ascending order; DO = descending order.
- E.g. list in ascending alphabetical order all customers who have an account at the bank

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	P.AO.	

- When sorting on multiple attributes, the sorting order is specified by including with each sort operator (AO or DO) an integer surrounded by parentheses.
- E.g. List all account numbers at the Perryridge branch in ascending alphabetic order with their respective account balances in descending order.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
	P.AO(1).	Perryridge	P.DO(2).





Aggregate Operations

- The aggregate operators are AVG, MAX, MIN, SUM, and CNT
- The above operators must be postfixed with “ALL” (e.g., SUM.ALL.or AVG.ALL._x) to ensure that duplicates are not eliminated.
- E.g. Find the total balance of all the accounts maintained at the Perryridge branch.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
		Perryridge	PSUM.ALL



Aggregate Operations (Cont.)

- UNQ is used to specify that we want to eliminate duplicates
- Find the total number of customers having an account at the bank.

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	P.CNT.UNQ.	





Query Examples

- Find the average balance at each branch.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
		P.G.	P.AVG.ALL_x

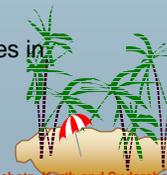
- The “G” in “P.G” is analogous to SQL’s **group by** construct
- The “ALL” in the “P.AVG.ALL” entry in the *balance* column ensures that all balances are considered
- To find the average account balance at only those branches where the average account balance is more than \$1,200, we simply add the condition box:

<i>conditions</i>
AVG.ALL_x > 1200



Query Example

- Find all customers who have an account at all branches located in Brooklyn.
 - Approach: for each customer, find the number of branches in Brooklyn at which they have accounts, and compare with total number of branches in Brooklyn
 - QBE does not provide subquery functionality, so both above tasks have to be combined in a single query.
 - Can be done for this query, but there are queries that require subqueries and cannot be expressed in QBE always be done.
- In the query on the next page
 - CNT.UNQ.ALL._w specifies the number of distinct branches in Brooklyn. Note: The variable _w is not connected to other variables in the query
 - CNT.UNQ.ALL._z specifies the number of distinct branches in Brooklyn at which customer x has an account.





Query Example (Cont.)

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
	PG..x	.y

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
	.y	.z	

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	.z	Brooklyn	
	.w	Brooklyn	

<i>conditions</i>
CNT.UNQ. _{.z} = CNT.UNQ. _{.w}



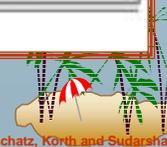
Modification of the Database – Deletion

- Deletion of tuples from a relation is expressed by use of a D. command. In the case where we delete information in only some of the columns, null values, specified by -, are inserted.
- Delete customer Smith

<i>customer</i>	<i>customer-name</i>	<i>customer-street</i>	<i>customer-city</i>
D.	Smith		

- Delete the *branch-city* value of the branch whose name is "Perryridge".

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	Perryridge	D.	





Deletion Query Examples

- Delete all loans with a loan amount between \$1300 and \$1500.
 - 🔑 For consistency, we have to delete information from loan and borrower tables

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
D.	-y		-x

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
D.		-y

<i>conditions</i>
-x = (≥ 1300 and ≤ 1500)



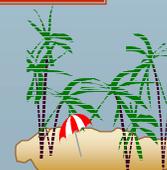
Deletion Query Examples (Cont.)

- Delete all accounts at branches located in Brooklyn.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
D.	-y	-x	

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
D.		-y

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	-x	Brooklyn	





Modification of the Database – Insertion

- Insertion is done by placing the I. operator in the query expression.
- Insert the fact that account A-9732 at the Perryridge branch has a balance of \$700.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
I.	A-9732	Perryridge	700



Modification of the Database – Insertion (Cont.)

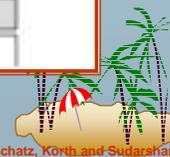
- Provide as a gift for all loan customers of the Perryridge branch, a new \$200 savings account for every loan account they have, with the loan number serving as the account number for the new savings account.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
I.	<i>x</i>	Perryridge	200

<i>depositor</i>	<i>customer-name</i>	<i>account-number</i>
I.	<i>y</i>	<i>x</i>

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
I.	<i>x</i>	Perryridge	

<i>borrower</i>	<i>customer-name</i>	<i>loan-number</i>
I.	<i>y</i>	<i>x</i>





Modification of the Database – Updates

- Use the U. operator to change a value in a tuple without changing *all* values in the tuple. QBE does not allow users to update the primary key fields.
- Update the asset value of the Perryridge branch to \$10,000,000.

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
	Perryridge		U.10000000

- Increase all balances by 5 percent.

<i>account</i>	<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
			U..r * 1.05



Microsoft Access QBE

- Microsoft Access supports a variant of QBE called Graphical Query By Example (GQBE)
- GQBE differs from QBE in the following ways
 - 🔑 Attributes of relations are listed vertically, one below the other, instead of horizontally
 - 🔑 Instead of using variables, lines (links) between attributes are used to specify that their values should be the same.
 - 📄 Links are added automatically on the basis of attribute name, and the user can then add or delete links
 - 📄 By default, a link specifies an inner join, but can be modified to specify outer joins.
 - 🔑 Conditions, values to be printed, as well as group by attributes are all specified together in a box called the **design grid**



An Example Query in Microsoft Access QBE

- Example query: Find the *customer-name*, *account-number* and *balance* for all accounts at the Perryridge branch

The screenshot shows the Microsoft Access Query By Example (QBE) interface. At the top, two tables are displayed: 'account' with fields 'account-number', 'branch-name', and 'balance'; and 'depositor' with fields 'customer-name' and 'account-number'. A line connects the 'account-number' field in the 'account' table to the 'account-number' field in the 'depositor' table. Below the tables is a grid for defining the query:

Field	customer-name	account-number	balance	branch-name
Table:	depositor	account	account	account
Sort:				
Show:	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Criteria:				"Perryridge"
or:				

An Aggregation Query in Access QBE

- Find the *name*, *street* and *city* of all customers who have more than one account at the bank

The screenshot shows the Microsoft Access Query By Example (QBE) interface. At the top, two tables are displayed: 'customer' with fields 'customer-name', 'customer-street', and 'customer-city'; and 'depositor' with fields 'customer-name' and 'account-number'. A line connects the 'customer-name' field in the 'customer' table to the 'customer-name' field in the 'depositor' table. Below the tables is a grid for defining the query:

Field	customer-name	customer-street	customer-city	account-number
Table:	customer	customer	customer	depositor
Total:	Group By	Group By	Group By	Count
Sort:				
Show:	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Criteria:				>1
or:				



Aggregation in Access QBE

- The row labeled **Total** specifies
 - 🔑 which attributes are group by attributes
 - 🔑 which attributes are to be aggregated upon (and the aggregate function).
 - 🔑 For attributes that are neither group by nor aggregated, we can still specify conditions by selecting **where** in the Total row and listing the conditions below
- As in SQL, if group by is used, only group by attributes and aggregate results can be output



Datalog

- Basic Structure
- Syntax of Datalog Rules
- Semantics of Nonrecursive Datalog
- Safety
- Relational Operations in Datalog
- Recursion in Datalog
- The Power of Recursion





Basic Structure

- Prolog-like logic-based language that allows recursive queries; based on first-order logic.
- A Datalog program consists of a set of *rules* that define views.
- Example: define a view relation *v1* containing account numbers and balances for accounts at the Perryridge branch with a balance of over \$700.

$$v1(A, B) :- \text{account}(A, \text{"Perryridge"}, B), B > 700.$$

- Retrieve the balance of account number "A-217" in the view relation *v1*.

$$? v1(\text{"A-217"}, B).$$

- To find account number and balance of all accounts in *v1* that have a balance greater than 800

$$? v1(A, B), B > 800$$


Example Queries

- Each rule defines a set of tuples that a view relation must contain.

🔑 E.g. $v1(A, B) :- \text{account}(A, \text{"Perryridge"}, B), B > 700$ is read as

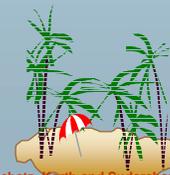
for all A, B

if $(A, \text{"Perryridge"}, B) \in \text{account}$ **and** $B > 700$

then $(A, B) \in v1$

- The set of tuples in a view relation is then defined as the union of all the sets of tuples defined by the rules for the view relation.

- Example:

$$\text{interest-rate}(A, 5) :- \text{account}(A, N, B), B < 10000$$
$$\text{interest-rate}(A, 6) :- \text{account}(A, N, B), B \geq 10000$$




Negation in Datalog

- Define a view relation c that contains the names of all customers who have a deposit but no loan at the bank:

$c(N) :- \text{depositor}(N, A), \text{not } \text{is-borrower}(N).$
 $\text{is-borrower}(N) :- \text{borrower}(N, L).$

- **NOTE:** using **not** $\text{borrower}(N, L)$ in the first rule results in a different meaning, namely there is some loan L for which N is not a borrower.

🔑 To prevent such confusion, we require all variables in negated "predicate" to also be present in non-negated predicates

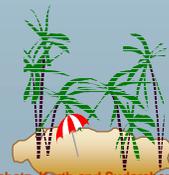


Named Attribute Notation

- Datalog rules use a positional notation, which is convenient for relations with a small number of attributes
- It is easy to extend Datalog to support named attributes.

🔑 E.g., $v1$ can be defined using named attributes as

$v1(\text{account-number } A, \text{balance } B) :-$
 $\text{account}(\text{account-number } A, \text{branch-name "Perryridge", balance } B),$
 $B > 700.$





Formal Syntax and Semantics of Datalog

- We formally define the syntax and semantics (meaning) of Datalog programs, in the following steps
 1. We define the syntax of predicates, and then the syntax of rules
 2. We define the semantics of individual rules
 3. We define the semantics of non-recursive programs, based on a layering of rules
 4. It is possible to write rules that can generate an infinite number of tuples in the view relation. To prevent this, we define what rules are “safe”. Non-recursive programs containing only safe rules can only generate a finite number of answers.
 5. It is possible to write recursive programs whose meaning is unclear. We define what recursive programs are acceptable, and define their meaning.

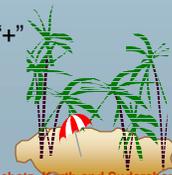


Syntax of Datalog Rules

- A *positive literal* has the form

$$p(t_1, t_2 \dots, t_n)$$
 - ☞ p is the name of a relation with n attributes
 - ☞ each t_i is either a constant or variable
- A *negative literal* has the form

$$\text{not } p(t_1, t_2 \dots, t_n)$$
- Comparison operations are treated as positive predicates
 - ☞ E.g. $X > Y$ is treated as a predicate $>(X, Y)$
 - ☞ “ $>$ ” is conceptually an (infinite) relation that contains all pairs of values such that the first value is greater than the second value
- Arithmetic operations are also treated as predicates
 - ☞ E.g. $A = B + C$ is treated as $+(B, C, A)$, where the relation “ $+$ ” contains all triples such that the third value is the sum of the first two





Syntax of Datalog Rules (Cont.)

- Rules are built out of literals and have the form:

$$p(t_1, t_2, \dots, t_n) :- \underbrace{L_1, L_2, \dots, L_m}_{\text{head}}$$

- each of the L_i 's is a literal
- head – the literal $p(t_1, t_2, \dots, t_n)$
- body – the rest of the literals

- A **fact** is a rule with an empty body, written in the form:

$$p(v_1, v_2, \dots, v_n).$$

- indicates tuple (v_1, v_2, \dots, v_n) is in relation p

- A **Datalog program** is a set of rules



Semantics of a Rule

- A **ground instantiation** of a rule (or simply **instantiation**) is the result of replacing each variable in the rule by some constant.

- Eg. Rule defining $v1$

$$v1(A,B) :- \text{account}(A, \text{"Perryridge"}, B), B > 700.$$

- An instantiation above rule:

$$v1(\text{"A-217"}, 750) :- \text{account}(\text{"A-217"}, \text{"Perryridge"}, 750), 750 > 700.$$

- The body of rule instantiation R' is **satisfied** in a set of facts (database instance) I if

- For each positive literal $q_i(v_{i,1}, \dots, v_{i,n_i})$ in the body of R' , I contains the fact $q_i(v_{i,1}, \dots, v_{i,n_i})$.
- For each negative literal **not** $q_j(v_{j,1}, \dots, v_{j,n_j})$ in the body of R' , I does not contain the fact $q_j(v_{j,1}, \dots, v_{j,n_j})$.





Semantics of a Rule (Cont.)

- We define the set of facts that can be **inferred** from a given set of facts I using rule R as:

$$\text{infer}(R, I) = \{p(t_1, \dots, t_n) \mid \text{there is a ground instantiation } R' \text{ of } R \text{ where } p(t_1, \dots, t_n) \text{ is the head of } R', \text{ and the body of } R' \text{ is satisfied in } I\}$$

- Given an set of rules $\mathfrak{R} = \{R_1, R_2, \dots, R_n\}$, we define

$$\text{infer}(\mathfrak{R}, I) = \text{infer}(R_1, I) \cup \text{infer}(R_2, I) \cup \dots \cup \text{infer}(R_n, I)$$


Layering of Rules

- Define the interest on each account in Perryridge

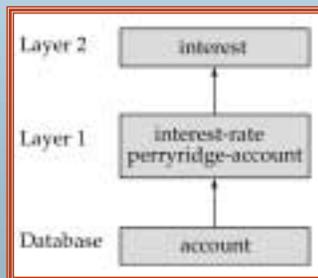
$$\text{interest}(A, I) :- \text{perryridge-account}(A, B), \text{interest-rate}(A, R), I = B * R / 100.$$

$$\text{perryridge-account}(A, B) :- \text{account}(A, \text{"Perryridge"}, B).$$

$$\text{interest-rate}(A, 5) :- \text{account}(N, A, B), B < 10000.$$

$$\text{interest-rate}(A, 6) :- \text{account}(N, A, B), B \geq 10000.$$

- Layering of the view relations





Layering Rules (Cont.)

Formally:

- A relation is a layer 1 if all relations used in the bodies of rules defining it are stored in the database.
- A relation is a layer 2 if all relations used in the bodies of rules defining it are either stored in the database, or are in layer 1.
- A relation p is in layer $i + 1$ if
 - ☞ it is not in layers 1, 2, ..., i
 - ☞ all relations used in the bodies of rules defining a p are either stored in the database, or are in layers 1, 2, ..., i

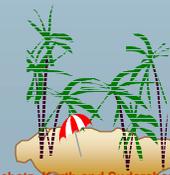


Semantics of a Program

Let the layers in a given program be 1, 2, ..., n . Let \mathfrak{R}_i denote the set of all rules defining view relations in layer i .

- Define I_0 = set of facts stored in the database.
- Recursively define $I_{i+1} = I_i \cup \text{infer}(\mathfrak{R}_{i+1}, I_i)$
- The set of facts in the view relations defined by the program (also called the semantics of the program) is given by the set of facts I_n corresponding to the highest layer n .

Note: Can instead define semantics using view expansion like in relational algebra, but above definition is better for handling extensions such as recursion.





Safety

- It is possible to write rules that generate an infinite number of answers.

$$gt(X, Y) :- X > Y$$

$$not-in-loan(B, L) :- \text{not } loan(B, L)$$

To avoid this possibility Datalog rules must satisfy the following conditions.

- Every variable that appears in the head of the rule also appears in a non-arithmetic positive literal in the body of the rule.
 - This condition can be weakened in special cases based on the semantics of arithmetic predicates, for example to permit the rule

$$p(A) :- q(B), A = B + 1$$
- Every variable appearing in a negative literal in the body of the rule also appears in some positive literal in the body of the rule.



Relational Operations in Datalog

- Project out attribute *account-name* from *account*.

$$query(A) :- account(A, N, B).$$

- Cartesian product of relations r_1 and r_2 .

$$query(X_1, X_2, \dots, X_n, Y_1, Y_2, \dots, Y_m) :-$$

$$r_1(X_1, X_2, \dots, X_n), r_2(Y_1, Y_2, \dots, Y_m).$$

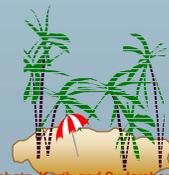
- Union of relations r_1 and r_2 .

$$query(X_1, X_2, \dots, X_n) :- r_1(X_1, X_2, \dots, X_n),$$

$$query(X_1, X_2, \dots, X_n) :- r_2(X_1, X_2, \dots, X_n),$$

- Set difference of r_1 and r_2 .

$$query(X_1, X_2, \dots, X_n) :- r_1(X_1, X_2, \dots, X_n),$$

$$\text{not } r_2(X_1, X_2, \dots, X_n),$$




Updates in Datalog

- Some Datalog extensions support database modification using + or – in the rule head to indicate insertion and deletion.
- E.g. to transfer all accounts at the Perryridge branch to the Johnstown branch, we can write
 - + account(A, “Johnstown”, B) :- account (A, “Perryridge”, B).
 - account(A, “Perryridge”, B) :- account (A, “Perryridge”, B)



Recursion in Datalog

- Suppose we are given a relation $manager(X, Y)$ containing pairs of names X, Y such that Y is a manager of X (or equivalently, X is a direct employee of Y).
- Each manager may have direct employees, as well as indirect employees
 - 🔑 Indirect employees of a manager, say Jones, are employees of people who are direct employees of Jones, or recursively, employees of people who are indirect employees of Jones
- Suppose we wish to find all (direct and indirect) employees of manager Jones. We can write a recursive Datalog program.
 - $empl-jones(X) :- manager(X, Jones).$
 - $empl-jones(X) :- manager(X, Y), empl-jones(Y).$





Semantics of Recursion in Datalog

- Assumption (for now): **program contains no negative literals**
- The view relations of a recursive program containing a set of rules \mathcal{R} are defined to contain exactly the set of facts I computed by the iterative procedure *Datalog-Fixpoint*

```

procedure Datalog-Fixpoint
   $I$  = set of facts in the database
  repeat
     $Old\_I = I$ 
     $I = I \cup infer(\mathcal{R}, I)$ 
  until  $I = Old\_I$ 

```

- At the end of the procedure, $infer(\mathcal{R}, I) \subseteq I$
 - 🔑 $infer(\mathcal{R}, I) = I$ if we consider the database to be a set of facts that are part of the program
- I is called a **fixed point** of the program.



Example of Datalog-FixPoint Iteration

<i>employee-name</i>	<i>manager-name</i>
Alon	Barinsky
Barinsky	Estovar
Corbin	Duarte
Duarte	Jones
Estovar	Jones
Jones	Klinger
Rensal	Klinger

Iteration number	Tuples in <i>empl-jones</i>
0	
1	(Duarte), (Estovar)
2	(Duarte), (Estovar), (Barinsky), (Corbin)
3	(Duarte), (Estovar), (Barinsky), (Corbin), (Alon)
4	(Duarte), (Estovar), (Barinsky), (Corbin), (Alon)





A More General View

- Create a view relation *empl* that contains every tuple (X, Y) such that X is directly or indirectly managed by Y .

$empl(X, Y) :- manager(X, Y).$
 $empl(X, Y) :- manager(X, Z), empl(Z, Y)$

- Find the direct and indirect employees of Jones.

? $empl(X, \text{"Jones"})$.

- Can define the view *empl* in another way too:

$empl(X, Y) :- manager(X, Y).$
 $empl(X, Y) :- empl(X, Z), manager(Z, Y).$



The Power of Recursion

- Recursive views make it possible to write queries, such as transitive closure queries, that cannot be written without recursion or iteration.
 - 🔗 Intuition: Without recursion, a non-recursive non-iterative program can perform only a fixed number of joins of *manager* with itself
 - 📖 This can give only a fixed number of levels of managers
 - 📖 Given a program we can construct a database with a greater number of levels of managers on which the program will not work





Recursion in SQL

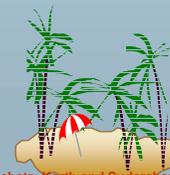
- SQL:1999 permits recursive view definition
- E.g. query to find all employee-manager pairs

```
with recursive empl (emp, mgr) as (  
    select emp, mgr  
    from manager  
union  
    select manager.emp, empl.mgr  
    from manager, empl  
    where manager.mgr = empl.emp )  
select *  
from empl
```



Monotonicity

- A view V is said to be **monotonic** if given any two sets of facts I_1 and I_2 such that $I_1 \subseteq I_2$, then $E_V(I_1) \subseteq E_V(I_2)$, where E_V is the expression used to define V .
- A set of rules R is said to be monotonic if $I_1 \subseteq I_2$ implies $infer(R, I_1) \subseteq infer(R, I_2)$.
- Relational algebra views defined using only the operations: Π , σ , \times , \cup , \cap , and ρ (as well as operations like natural join defined in terms of these operations) are monotonic.
- Relational algebra views defined using – may not be monotonic.
- Similarly, Datalog programs without negation are monotonic, but Datalog programs with negation may not be monotonic.





Non-Monotonicity

- Procedure *Datalog-Fixpoint* is sound provided the rules in the program are monotonic.
 - 📌 Otherwise, it may make some inferences in an iteration that cannot be made in a later iteration. E.g. given the rules
 - $a :- \text{not } b.$
 - $b :- c.$
 - $c.$
 Then a can be inferred initially, before b is inferred, but not later.
- We can extend the procedure to handle negation so long as the program is “stratified”: intuitively, so long as negation is not mixed with recursion

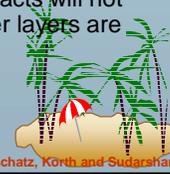


Stratified Negation

- A Datalog program is said to be stratified if its predicates can be given layer numbers such that
 1. For all positive literals, say q , in the body of any rule with head, say, p

$$p(..) :- \dots, q(..), \dots$$
 then the layer number of p is greater than or equal to the layer number of q
 2. Given any rule with a negative literal

$$p(..) :- \dots, \text{not } q(..), \dots$$
 then the layer number of p is strictly greater than the layer number of q
- Stratified programs do not have recursion mixed with negation
- We can define the semantics of stratified programs layer by layer, from the bottom-most layer, using fixpoint iteration to define the semantics of each layer.
 - 📌 Since lower layers are handled before higher layers, their facts will not change, so each layer is monotonic once the facts for lower layers are fixed.





Non-Monotonicity (Cont.)

- There are useful queries that cannot be expressed by a stratified program
 - 📌 E.g., given information about the number of each subpart in each part, in a part-subpart hierarchy, find the total number of subparts of each part.
 - 📌 A program to compute the above query would have to mix aggregation with recursion
 - 📌 However, so long as the underlying data (part-subpart) has no cycles, it is possible to write a program that mixes aggregation with recursion, yet has a clear meaning
 - 📌 There are ways to evaluate some such classes of non-stratified programs



Forms and Graphical User Interfaces

- Most naive users interact with databases using form interfaces with graphical interaction facilities
 - 📌 Web interfaces are the most common kind, but there are many others
 - 📌 Forms interfaces usually provide mechanisms to check for correctness of user input, and automatically fill in fields given key values
 - 📌 Most database vendors provide convenient mechanisms to create forms interfaces, and to link form actions to database actions performed using SQL





Report Generators

- Report generators are tools to generate human-readable summary reports from a database
 - 📌 They integrate database querying with creation of formatted text and graphical charts
 - 📌 Reports can be defined once and executed periodically to get current information from the database.
 - 📌 Example of report (next page)
 - 📌 Microsoft's Object Linking and Embedding (OLE) provides a convenient way of embedding objects such as charts and tables generated from the database into other objects such as Word documents.



A Formatted Report

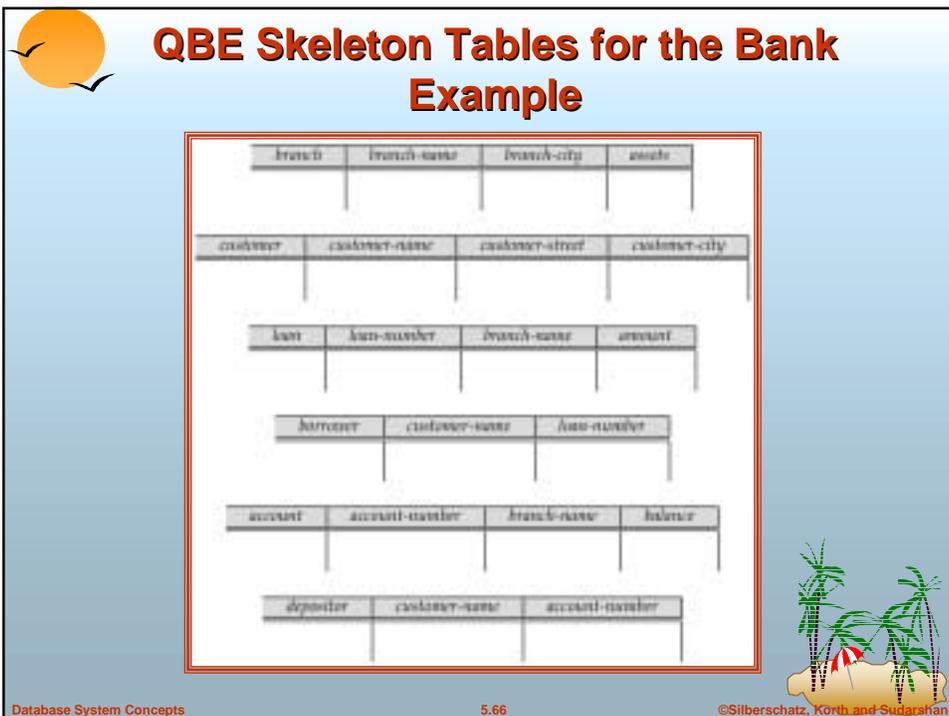
Acme Supply Company Inc.
Quarterly Sales Report

Period: Jan. 1 to March 31, 2001

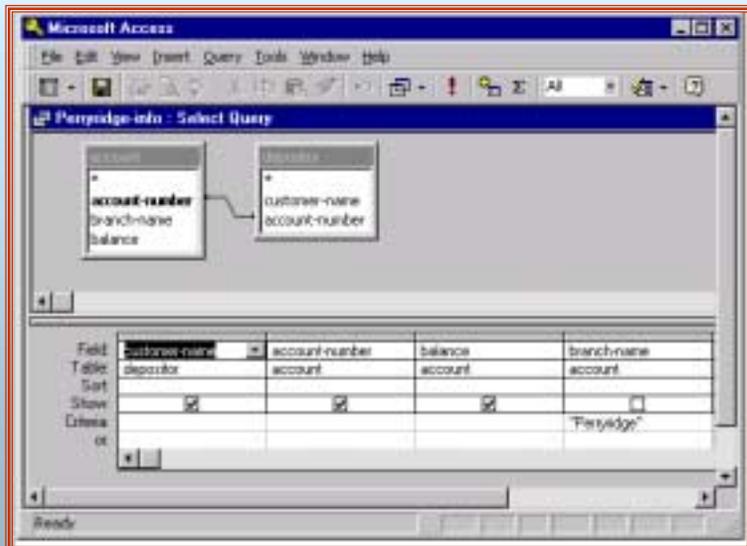
Region	Category	Sales	Subtotal
North	Computer Hardware	1,000,000	1,500,000
	Computer Software	500,000	
	All categories		
South	Computer Hardware	200,000	600,000
	Computer Software	400,000	
	All categories		
Total Sales			2,100,000



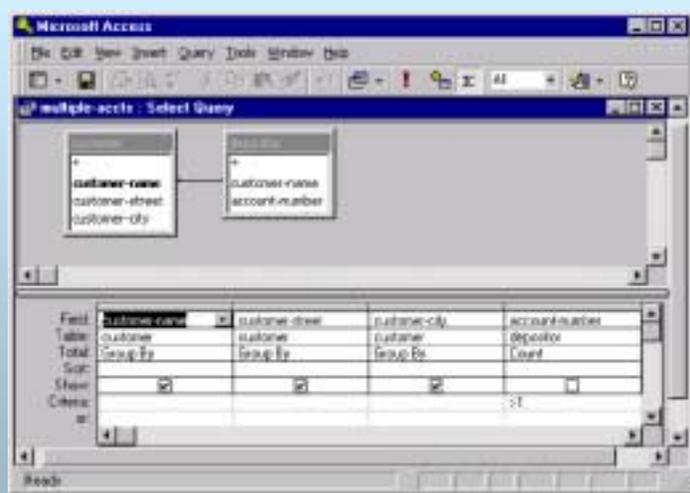
End of Chapter



An Example Query in Microsoft Access QBE



An Aggregation Query in Microsoft Access QBE





The *account* Relation

<i>account-number</i>	<i>branch-name</i>	<i>balance</i>
A-101	Downtown	500
A-215	Mianus	700
A-102	Perryridge	400
A-305	Round Hill	350
A-201	Perryridge	900
A-222	Redwood	700
A-217	Perryridge	750



The *v1* Relation

<i>account-number</i>	<i>balance</i>
A-201	900
A-217	750





Result of $\text{infer}(R, I)$

<i>account-number</i>	<i>balance</i>
A-201	900
A-217	750



<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	P.	Perryridge	

<i>loan</i>	<i>loan-number</i>	<i>branch-name</i>	<i>amount</i>
	.x	Perryridge	

<i>branch</i>	<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>
L.	Capital	Queens	

<i>conditions</i>
$.y \geq 2 * .z$

